

(Open book exam)

Problem

(20 marks)

A). Estimate the flow efficiency using the following data:

$$\begin{array}{lll} \beta_o = 1.226 \text{ bbl/STB} & \mu_o = 3.75 \text{ cp} & k = 19.1 \text{ md} \\ h = 67 \text{ ft} & r_w = 0.3 \text{ ft} & p_{wf} = 2309 \text{ psi} \\ P_{avg} = 3137 \text{ psi} & q_o = 105 \text{ STB/d} & s = 8.2 \end{array}$$

B). An oil well drilled in a field with uniform 40-acre square drilling pattern has produced for 10 days with a constant pressure decline of 48 psi/day. The gas-oil ratio has been constant during the production. The well was damaged out due to build-up test analysis and skin factor estimated to be 2.43. The flowing bottom-hole pressure is 1123 psi. The rock and fluid data are as follows :

$$\begin{array}{lll} \phi = 0.1 & h = 40 \text{ ft} & \mu_o = 2.0 \text{ cp} \\ C_t = 10 \times 10^{-6} \text{ psi}^{-1} & r_w = 4.0 \text{ in.} & \beta_o = 1.31 \text{ bbl/STB} \\ k = 82.5 \text{ md} & & \end{array}$$

Estimate:

- a). drainage well radius.                      b). oil flow rate.  
c). average reservoir pressure.              d). pressure drop due to well damage.  
e). At what type of flow regime is this well producing?

Problem 2

(20 marks)

A). The Ei-solution to the diffusivity equation is given by the following formula:

$$p(r, t) = p_i + \left[ \frac{70.6QB\mu}{kh} \right] \text{Ei} \left[ \frac{-948\phi\mu c_t r^2}{kt} \right]$$

Prove that the above equation can be expressed by this formula:

$$p_D = -\frac{1}{2} \text{Ei} \left( -\frac{r_D^2}{4t_D} \right)$$

B). Using the following fluid and rock properties of a producing well :

$$\begin{array}{llll} P_i = 5651 \text{ psia} & P_{wf} = 3500 \text{ psia} & k = 8.2 \text{ md} & h = 53 \text{ ft} \\ \phi = 19 \% & \mu_o = 1.7 \text{ cp} & r_w = 0.328 \text{ ft} & \beta_o = 1.1 \text{ bbl/STB} \\ C_t = 1.29 \times 10^{-5} \text{ psi}^{-1} & & & \end{array}$$

to develop a relationship between production rate and time assuming unsteady state flow condition .

C). An oil well has initial pressure of 3500 psia and producing at a constant flow rate of 300 STB/day under unsteady state flow conditions. The rock and fluid characteristics are:

$$\begin{array}{lll} k = 120 \text{ md} & \beta_o = 1.2 \text{ bbl/STB} & \mu_o = 2 \text{ cp} \\ s = 3 & h = 20 \text{ ft} & \phi = 0.25 \\ r_w = 0.328 \text{ ft} & C_t = 20 \times 10^{-6} \text{ psi}^{-1} & \end{array}$$

Calculate : a). pressure after 20 hrs at 100 ft away from the wellbore.

b). flowing bottom-hole pressure after 20 hours.

c). flowing bottom-hole pressure after 50 hours using  $P_D$ -method.

**Problem 3**

(20 marks)

A). Gas flow rate has recorded against apparent skin factor as follows:

$q_g$ mmscf/day	$S'$
5	7
10	11
20	19

Calculate

- 1). the true skin factor " $S$ ", and
  - 2). turbulent factor " $D$ ".
  - 3). Apparent skin factor " $S'$ " if  $q_g = 15$  mmscf/d
- B). A gas well is producing at a constant rate of 8 mm scf/day under steady state flow conditions. The following data is available:

$$\begin{aligned}
 K &= 50 \text{ md} & h &= 15 \text{ ft} & \phi &= 0.20 & P_i &= 2000 \text{ psia} \\
 T &= 140^\circ \text{f} & r_w &= 0.333 \text{ ft} & & & & \\
 r_e &= 1000 \text{ ft} & & & & & & 
 \end{aligned}$$

The gas properties are tabulated below :

$P, \text{psia}$	$\mu_g, \text{cp}$	$z$
400	0.01286	0.937
800	0.01390	0.883
1200	0.01530	0.832
1600	0.01680	0.794
2000	0.01840	0.770

- 1). Plot  $\psi(P)$  versus pressure, and find the value of  $\psi(p)$  at  $P = 1000$  psia
- 2). Calculate the flowing bottom-hole pressure using:
  - a). pseudopressure method.
  - b). squared- pressure method .

**Good Luck**