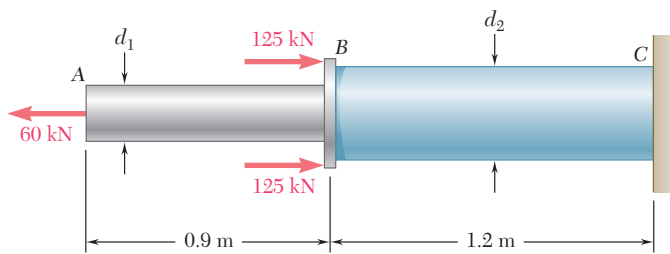


# CHAPTER 1

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**PROBLEM 1.1**

Two solid cylindrical rods  $AB$  and  $BC$  are welded together at  $B$  and loaded as shown. Knowing that  $d_1 = 30$  mm and  $d_2 = 50$  mm, find the average normal stress at the midsection of (a) rod  $AB$ , (b) rod  $BC$ .

**SOLUTION**(a) Rod  $AB$ :

Force:  $P = 60 \times 10^3$  N tension

Area:  $A = \frac{\pi}{4} d_1^2 = \frac{\pi}{4} (30 \times 10^{-3})^2 = 706.86 \times 10^{-6} \text{ m}^2$

Normal stress:  $\sigma_{AB} = \frac{P}{A} = \frac{60 \times 10^3}{706.86 \times 10^{-6}} = 84.882 \times 10^6 \text{ Pa}$   $\sigma_{AB} = 84.9 \text{ MPa} \blacktriangleleft$

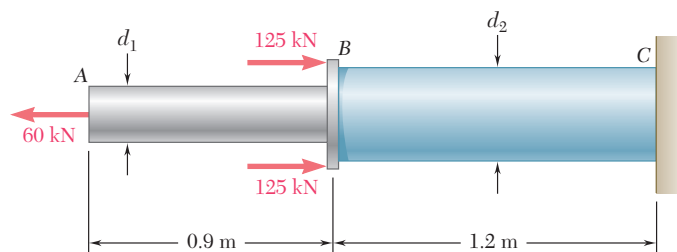
(b) Rod  $BC$ :

Force:  $P = 60 \times 10^3 - (2)(125 \times 10^3) = -190 \times 10^3$  N

Area:  $A = \frac{\pi}{4} d_2^2 = \frac{\pi}{4} (50 \times 10^{-3})^2 = 1.96350 \times 10^{-3} \text{ m}^2$

Normal stress:  $\sigma_{BC} = \frac{P}{A} = \frac{-190 \times 10^3}{1.96350 \times 10^{-3}} = -96.766 \times 10^6 \text{ Pa}$   $\sigma_{BC} = -96.8 \text{ MPa} \blacktriangleleft$

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Full file at <https://TestbankDirect.eu/>**PROBLEM 1.2**

Two solid cylindrical rods  $AB$  and  $BC$  are welded together at  $B$  and loaded as shown. Knowing that the average normal stress must not exceed 150 MPa in either rod, determine the smallest allowable values of the diameters  $d_1$  and  $d_2$ .

**SOLUTION**(a) Rod  $AB$ :

Force:  $P = 60 \times 10^3 \text{ N}$

Stress:  $\sigma_{AB} = 150 \times 10^6 \text{ Pa}$

Area:  $A = \frac{\pi}{4} d_1^2$

$$\sigma_{AB} = \frac{P}{A} \quad \therefore \quad A = \frac{P}{\sigma_{AB}}$$

$$\frac{\pi}{4} d_1^2 = \frac{P}{\sigma_{AB}}$$

$$d_1^2 = \frac{4P}{\pi\sigma_{AB}} = \frac{(4)(60 \times 10^3)}{\pi(150 \times 10^6)} = 509.30 \times 10^{-6} \text{ m}^2$$

$$d_1 = 22.568 \times 10^{-3} \text{ m}$$

$$d_1 = 22.6 \text{ mm} \blacktriangleleft$$

(b) Rod  $BC$ :

Force:  $P = 60 \times 10^3 - (2)(125 \times 10^3) = -190 \times 10^3 \text{ N}$

Stress:  $\sigma_{BC} = -150 \times 10^6 \text{ Pa}$

Area:  $A = \frac{\pi}{4} d_2^2$

$$\sigma_{BC} = \frac{P}{A} = \frac{4P}{\pi d_2^2}$$

$$d_2^2 = \frac{4P}{\pi\sigma_{BC}} = \frac{(4)(-190 \times 10^3)}{\pi(-150 \times 10^6)} = 1.61277 \times 10^{-3} \text{ m}^2$$

$$d_2 = 40.159 \times 10^{-3} \text{ m}$$

$$d_2 = 40.2 \text{ mm} \blacktriangleleft$$

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### PROBLEM 1.3

Two solid cylindrical rods  $AB$  and  $BC$  are welded together at  $B$  and loaded as shown. Knowing that  $P = 10$  kips, find the average normal stress at the midsection of (a) rod  $AB$ , (b) rod  $BC$ .

**SOLUTION**(a) Rod  $AB$ :

$$P = 12 + 10 = 22 \text{ kips}$$

$$A = \frac{\pi}{4} d_1^2 = \frac{\pi}{4} (1.25)^2 = 1.22718 \text{ in}^2$$

$$\sigma_{AB} = \frac{P}{A} = \frac{22}{1.22718} = 17.927 \text{ ksi}$$

$$\sigma_{AB} = 17.93 \text{ ksi} \quad \blacktriangleleft$$

(b) Rod  $BC$ :

$$P = 10 \text{ kips}$$

$$A = \frac{\pi}{4} d_2^2 = \frac{\pi}{4} (0.75)^2 = 0.44179 \text{ in}^2$$

$$\sigma_{AB} = \frac{P}{A} = \frac{10}{0.44179} = 22.635 \text{ ksi}$$

$$\sigma_{AB} = 22.6 \text{ ksi} \quad \blacktriangleleft$$

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**PROBLEM 1.4**

Two solid cylindrical rods  $AB$  and  $BC$  are welded together at  $B$  and loaded as shown. Determine the magnitude of the force  $\mathbf{P}$  for which the tensile stresses in rods  $AB$  and  $BC$  are equal.

**SOLUTION**(a) Rod  $AB$ :

$$P = P + 12 \text{ kips}$$

$$A = \frac{\pi d^2}{4} = \frac{\pi}{4} (1.25 \text{ in.})^2$$

$$A = 1.22718 \text{ in}^2$$

$$\sigma_{AB} = \frac{P + 12 \text{ kips}}{1.22718 \text{ in}^2}$$

(b) Rod  $BC$ :

$$P = P$$

$$A = \frac{\pi}{4} d^2 = \frac{\pi}{4} (0.75 \text{ in.})^2$$

$$A = 0.44179 \text{ in}^2$$

$$\sigma_{BC} = \frac{P}{0.44179 \text{ in}^2}$$

$$\sigma_{AB} = \sigma_{BC}$$

$$\frac{P + 12 \text{ kips}}{1.22718 \text{ in}^2} = \frac{P}{0.44179 \text{ in}^2}$$

$$5.3015 = 0.78539P$$

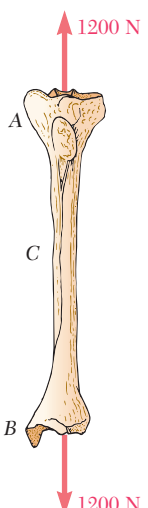
$$P = 6.75 \text{ kips} \blacktriangleleft$$

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**PROBLEM 1.5**

A strain gage located at  $C$  on the surface of bone  $AB$  indicates that the average normal stress in the bone is 3.80 MPa when the bone is subjected to two 1200-N forces as shown. Assuming the cross section of the bone at  $C$  to be annular and knowing that its outer diameter is 25 mm, determine the inner diameter of the bone's cross section at  $C$ .

**SOLUTION**

$$\sigma = \frac{P}{A} \quad \therefore \quad A = \frac{P}{\sigma}$$

Geometry:  $A = \frac{\pi}{4}(d_1^2 - d_2^2)$

$$d_2^2 = d_1^2 - \frac{4A}{\pi} = d_1^2 - \frac{4P}{\pi\sigma}$$

$$d_2^2 = (25 \times 10^{-3})^2 - \frac{(4)(1200)}{\pi(3.80 \times 10^6)}$$

$$= 222.92 \times 10^{-6} \text{ m}^2$$

$$d_2 = 14.93 \times 10^{-3} \text{ m}$$

$$d_2 = 14.93 \text{ mm} \quad \blacktriangleleft$$

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The diagram shows a vertical rod suspended from a support at point A. The rod is divided into two sections: section AB of length  $a$  and diameter 15 mm, and section BC of length  $b$  and diameter 10 mm. The total length of the rod is 100 m. The support is at the top, and the rod hangs vertically.

**PROBLEM 1.6**

Two brass rods  $AB$  and  $BC$ , each of uniform diameter, will be brazed together at  $B$  to form a nonuniform rod of total length 100 m, which will be suspended from a support at  $A$  as shown. Knowing that the density of brass is  $8470 \text{ kg/m}^3$ , determine (a) the length of rod  $AB$  for which the maximum normal stress in  $ABC$  is minimum, (b) the corresponding value of the maximum normal stress.

**SOLUTION**

Areas:  $A_{AB} = \frac{\pi}{4}(15 \text{ mm})^2 = 176.715 \text{ mm}^2 = 176.715 \times 10^{-6} \text{ m}^2$

$A_{BC} = \frac{\pi}{4}(10 \text{ mm})^2 = 78.54 \text{ mm}^2 = 78.54 \times 10^{-6} \text{ m}^2$

From geometry,  $b = 100 - a$

Weights:  $W_{AB} = \rho g A_{AB} \ell_{AB} = (8470)(9.81)(176.715 \times 10^{-6})a = 14.683a$

$W_{BC} = \rho g A_{BC} \ell_{BC} = (8470)(9.81)(78.54 \times 10^{-6})(100 - a) = 652.59 - 6.526a$

Normal stresses:

At  $A$ ,  $P_A = W_{AB} + W_{BC} = 652.59 + 8.157a$  (1)

$\sigma_A = \frac{P_A}{A_{AB}} = 3.6930 \times 10^6 + 46.160 \times 10^3 a$

At  $B$ ,  $P_B = W_{BC} = 652.59 - 6.526a$  (2)

$\sigma_B = \frac{P_B}{A_{BC}} = 8.3090 \times 10^6 - 83.090 \times 10^3 a$

(a) Length of rod  $AB$ . The maximum stress in  $ABC$  is minimum when  $\sigma_A = \sigma_B$  or

$4.6160 \times 10^6 - 129.25 \times 10^3 a = 0$

$a = 35.71 \text{ m}$

$\ell_{AB} = a = 35.7 \text{ m} \blacktriangleleft$

(b) Maximum normal stress.

$\sigma_A = 3.6930 \times 10^6 + (46.160 \times 10^3)(35.71)$

$\sigma_B = 8.3090 \times 10^6 - (83.090 \times 10^3)(35.71)$

$\sigma_A = \sigma_B = 5.34 \times 10^6 \text{ Pa}$

$\sigma = 5.34 \text{ MPa} \blacktriangleleft$



**PROBLEM 1.7**

Each of the four vertical links has an  $8 \times 36$ -mm uniform rectangular cross section and each of the four pins has a 16-mm diameter. Determine the maximum value of the average normal stress in the links connecting (a) points  $B$  and  $D$ , (b) points  $C$  and  $E$ .

**SOLUTION**

Use bar  $ABC$  as a free body.

$$\Sigma M_C = 0 : (0.040)F_{BD} - (0.025 + 0.040)(20 \times 10^3) = 0$$

$$F_{BD} = 32.5 \times 10^3 \text{ N} \quad \text{Link } BD \text{ is in tension.}$$

$$\Sigma M_B = 0 : -(0.040)F_{CE} - (0.025)(20 \times 10^3) = 0$$

$$F_{CE} = -12.5 \times 10^3 \text{ N} \quad \text{Link } CE \text{ is in compression.}$$

Net area of one link for tension =  $(0.008)(0.036 - 0.016) = 160 \times 10^{-6} \text{ m}^2$

For two parallel links,  $A_{\text{net}} = 320 \times 10^{-6} \text{ m}^2$

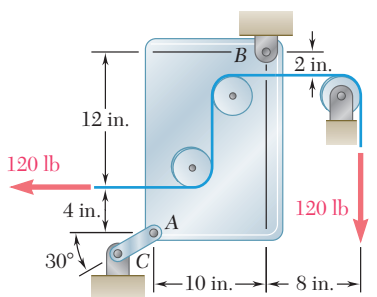
(a)  $\sigma_{BD} = \frac{F_{BD}}{A_{\text{net}}} = \frac{32.5 \times 10^3}{320 \times 10^{-6}} = 101.563 \times 10^6$   $\sigma_{BD} = 101.6 \text{ MPa} \blacktriangleleft$

Area for one link in compression =  $(0.008)(0.036) = 288 \times 10^{-6} \text{ m}^2$

For two parallel links,  $A = 576 \times 10^{-6} \text{ m}^2$

(b)  $\sigma_{CE} = \frac{F_{CE}}{A} = \frac{-12.5 \times 10^3}{576 \times 10^{-6}} = -21.701 \times 10^6$   $\sigma_{CE} = -21.7 \text{ MPa} \blacktriangleleft$

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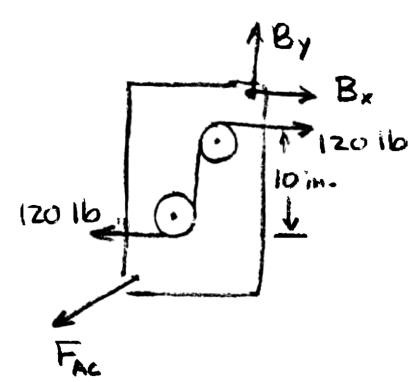


**PROBLEM 1.8**

Link AC has a uniform rectangular cross section  $\frac{1}{8}$  in. thick and 1 in. wide. Determine the normal stress in the central portion of the link.

**SOLUTION**

Use the plate together with two pulleys as a free body. Note that the cable tension causes at 1200 lb-in. clockwise couple to act on the body.



$$+\circlearrowleft \Sigma M_B = 0: \quad -(12 + 4)(F_{AC} \cos 30^\circ) + (10)(F_{AC} \sin 30^\circ) - 1200 \text{ lb} = 0$$

$$F_{AC} = -\frac{1200 \text{ lb}}{16 \cos 30^\circ - 10 \sin 30^\circ} = -135.500 \text{ lb}$$

Area of link AC:  $A = 1 \text{ in.} \times \frac{1}{8} \text{ in.} = 0.125 \text{ in}^2$

Stress in link AC:  $\sigma_{AC} = \frac{F_{AC}}{A} = -\frac{135.50}{0.125} = 1084 \text{ psi} = 1.084 \text{ ksi}$

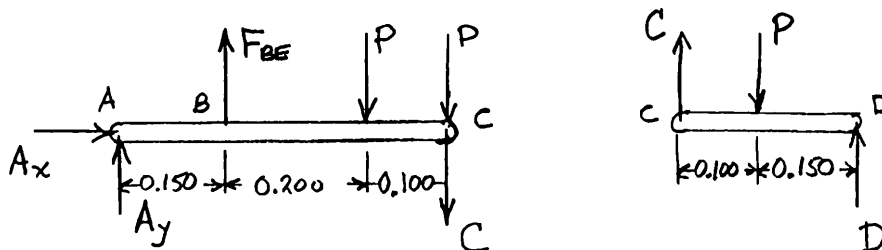
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**PROBLEM 1.9**

Three forces, each of magnitude  $P = 4 \text{ kN}$ , are applied to the mechanism shown. Determine the cross-sectional area of the uniform portion of rod  $BE$  for which the normal stress in that portion is  $+100 \text{ MPa}$ .

**SOLUTION**

Draw free body diagrams of  $AC$  and  $CD$ .



Free Body  $CD$ : 
$$+\circlearrowleft \Sigma M_D = 0: 0.150P - 0.250C = 0$$
  

$$C = 0.6P$$

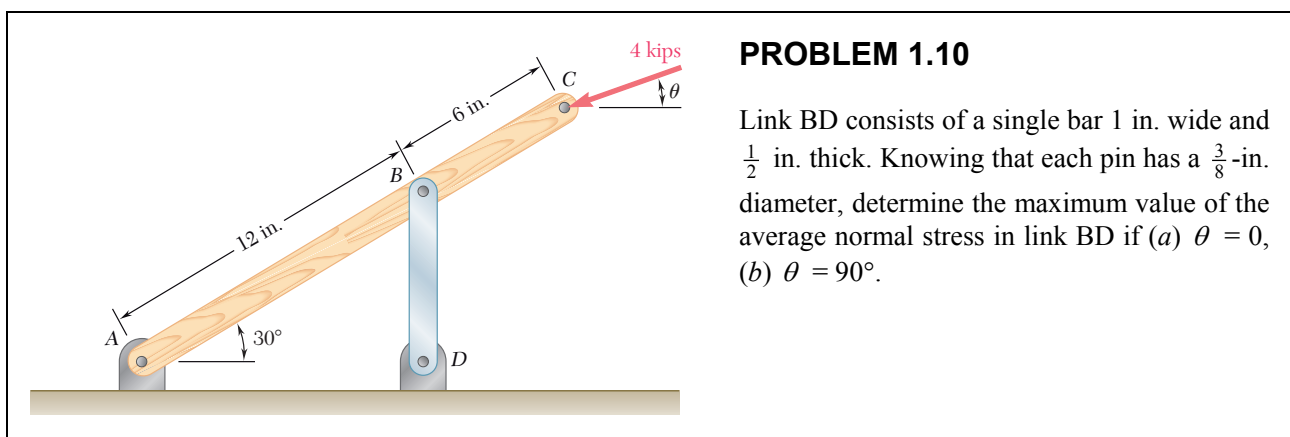
Free Body  $AC$ : 
$$+\circlearrowleft M_A = 0: 0.150F_{BE} - 0.350P - 0.450P - 0.450C = 0$$
  

$$F_{BE} = \frac{1.07}{0.150}P = 7.1333P = (7.133)(4 \text{ kN}) = 28.533 \text{ kN}$$

Required area of  $BE$ : 
$$\sigma_{BE} = \frac{F_{BE}}{A_{BE}}$$
  

$$A_{BE} = \frac{F_{BE}}{\sigma_{BE}} = \frac{28.533 \times 10^3}{100 \times 10^6} = 285.33 \times 10^{-6} \text{ m}^2$$

$$A_{BE} = 285 \text{ mm}^2 \blacktriangleleft$$

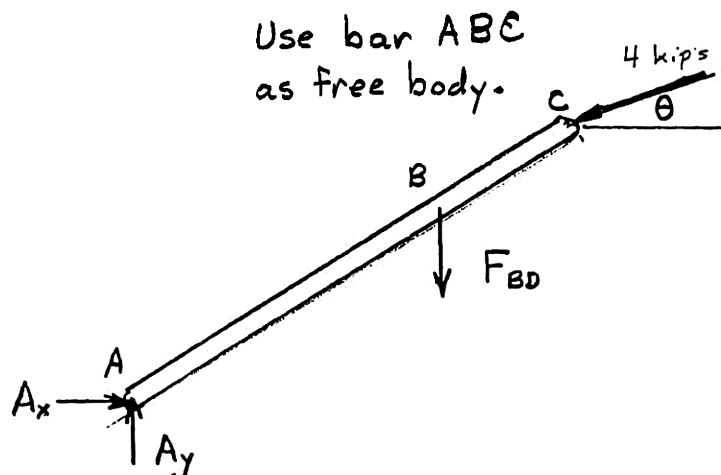


**PROBLEM 1.10**

Link BD consists of a single bar 1 in. wide and  $\frac{1}{2}$  in. thick. Knowing that each pin has a  $\frac{3}{8}$ -in. diameter, determine the maximum value of the average normal stress in link BD if (a)  $\theta = 0$ , (b)  $\theta = 90^\circ$ .

**SOLUTION**

Use bar *ABC* as a free body.



(a)  $\theta = 0$ .

$$+\curvearrowright \Sigma M_A = 0: (18 \sin 30^\circ)(4) - (12 \cos 30^\circ)F_{BD} = 0$$

$$F_{BD} = 3.4641 \text{ kips (tension)}$$

Area for tension loading:  $A = (b - d)t = \left(1 - \frac{3}{8}\right)\left(\frac{1}{2}\right) = 0.31250 \text{ in}^2$

Stress:  $\sigma = \frac{F_{BD}}{A} = \frac{3.4641 \text{ kips}}{0.31250 \text{ in}^2} \quad \sigma = 11.09 \text{ ksi} \blacktriangleleft$

(b)  $\theta = 90^\circ$ .

$$+\curvearrowright \Sigma M_A = 0: -(18 \cos 30^\circ)(4) - (12 \cos 30^\circ)F_{BD} = 0$$

$$F_{BD} = -6 \text{ kips i.e. compression.}$$

Area for compression loading:  $A = bt = (1)\left(\frac{1}{2}\right) = 0.5 \text{ in}^2$

Stress:  $\sigma = \frac{F_{BD}}{A} = \frac{-6 \text{ kips}}{0.5 \text{ in}^2} \quad \sigma = 12.00 \text{ ksi} \blacktriangleleft$

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**PROBLEM 1.11**

For the Pratt bridge truss and loading shown, determine the average normal stress in member  $BE$ , knowing that the cross-sectional area of that member is  $5.87 \text{ in}^2$ .

**SOLUTION**

Use entire truss as free body.

$$+\circlearrowleft \Sigma M_H = 0: (9)(80) + (18)(80) + (27)(80) - 36A_y = 0$$

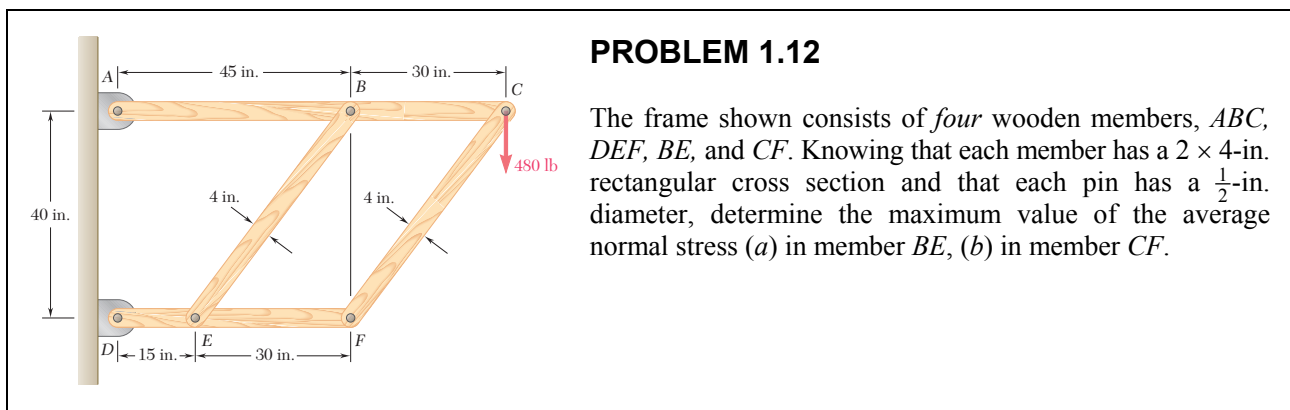
$$A_y = 120 \text{ kips}$$

Use portion of truss to the left of a section cutting members  $BD$ ,  $BE$ , and  $CE$ .

$$+\uparrow \Sigma F_y = 0: 120 - 80 - \frac{12}{15}F_{BE} = 0 \quad \therefore F_{BE} = 50 \text{ kips}$$

$$\sigma_{BE} = \frac{F_{BE}}{A} = \frac{50 \text{ kips}}{5.87 \text{ in}^2}$$

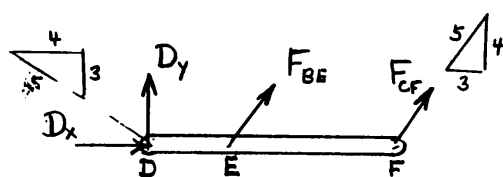
$$\sigma_{BE} = 8.52 \text{ ksi} \quad \blacktriangleleft$$



**PROBLEM 1.12**

The frame shown consists of *four* wooden members, *ABC*, *DEF*, *BE*, and *CF*. Knowing that each member has a  $2 \times 4$ -in. rectangular cross section and that each pin has a  $\frac{1}{2}$ -in. diameter, determine the maximum value of the average normal stress (a) in member *BE*, (b) in member *CF*.

**SOLUTION**



Add support reactions to figure as shown.

Using entire frame as free body,

$$\begin{aligned} \Sigma M_A = 0: \quad 40D_x - (45 + 30)(480) &= 0 \\ D_x &= 900 \text{ lb} \end{aligned}$$

Use member DEF as free body.

Reaction at D must be parallel to  $F_{BE}$  and  $F_{CF}$ .

$$D_y = \frac{4}{3}D_x = 1200 \text{ lb}$$

$$\Sigma M_F = 0: \quad - (30)\left(\frac{4}{5}F_{BE}\right) - (30 + 15)D_y = 0$$

$$F_{BE} = -2250 \text{ lb}$$

$$\Sigma M_E = 0: \quad (30)\left(\frac{4}{5}F_{CF}\right) - (15)D_y = 0$$

$$F_{CF} = 750 \text{ lb}$$

Stress in compression member *BE*:

$$\text{Area: } A = 2 \text{ in.} \times 4 \text{ in.} = 8 \text{ in}^2$$

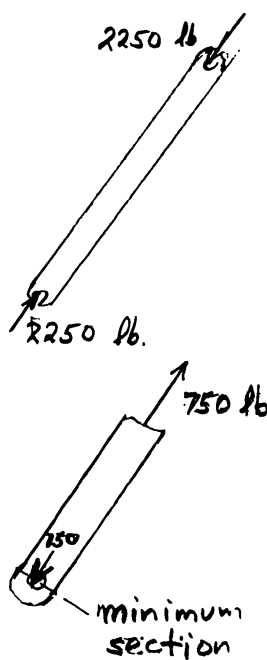
$$(a) \quad \sigma_{BE} = \frac{F_{BE}}{A} = \frac{-2250}{8} \quad \sigma_{BE} = -281 \text{ psi} \quad \blacktriangleleft$$

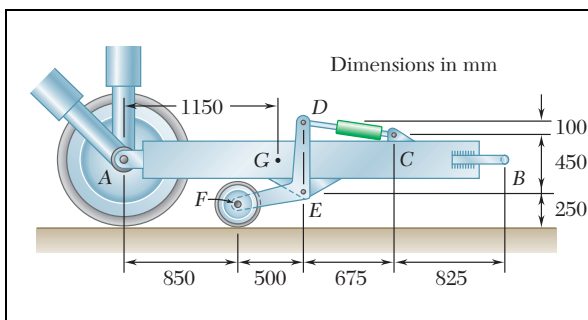
Minimum section area occurs at pin.

$$A_{\min} = (2)(4.0 - 0.5) = 7.0 \text{ in}^2$$

$$(b) \quad \sigma_{CF} = \frac{F_{CF}}{A_{\min}} = \frac{750}{7.0} \quad \sigma_{CF} = 107.1 \text{ psi} \quad \blacktriangleleft$$

Stress in tension member *CF*:

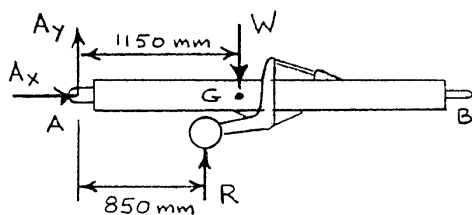




**PROBLEM 1.13**

An aircraft tow bar is positioned by means of a single hydraulic cylinder connected by a 25-mm-diameter steel rod to two identical arm-and-wheel units *DEF*. The mass of the entire tow bar is 200 kg, and its center of gravity is located at *G*. For the position shown, determine the normal stress in the rod.

**SOLUTION**

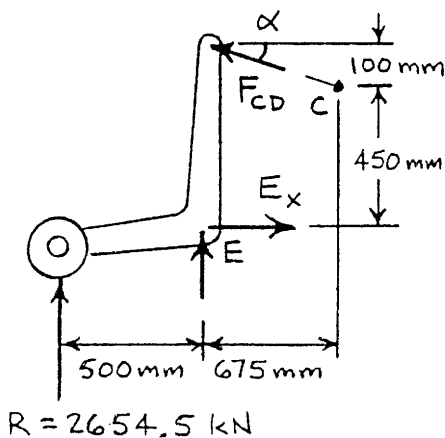


FREE BODY – ENTIRE TOW BAR:

$$W = (200 \text{ kg})(9.81 \text{ m/s}^2) = 1962.00 \text{ N}$$

$$+\circlearrowleft \Sigma M_A = 0: 850R - 1150(1962.00 \text{ N}) = 0$$

$$R = 2654.5 \text{ N}$$



FREE BODY – BOTH ARM & WHEEL UNITS:

$$R = 2654.5 \text{ kN}$$

$$\tan \alpha = \frac{100}{675} \quad \alpha = 8.4270^\circ$$

$$+\circlearrowleft \Sigma M_E = 0: (F_{CD} \cos \alpha)(550) - R(500) = 0$$

$$F_{CD} = \frac{500}{550 \cos 8.4270^\circ} (2654.5 \text{ N})$$

$$= 2439.5 \text{ N (comp.)}$$

$$\sigma_{CD} = -\frac{F_{CD}}{A_{CD}} = -\frac{2439.5 \text{ N}}{\pi(0.0125 \text{ m})^2}$$

$$= -4.9697 \times 10^6 \text{ Pa} \quad \sigma_{CD} = -4.97 \text{ MPa} \blacktriangleleft$$

**PROBLEM 1.14**

Two hydraulic cylinders are used to control the position of the robotic arm  $ABC$ . Knowing that the control rods attached at  $A$  and  $D$  each have a 20-mm diameter and happen to be parallel in the position shown, determine the average normal stress in (a) member  $AE$ , (b) member  $DG$ .

**SOLUTION**

Use member  $ABC$  as free body.

Use member  $ABC$  as free body.

$$+\curvearrowright \sum M_B = 0: (0.150) \frac{4}{5} F_{AE} - (0.600)(800) = 0$$

$$F_{AE} = 4 \times 10^3 \text{ N}$$

Area of rod in member  $AE$  is  $A = \frac{\pi}{4} d^2 = \frac{\pi}{4} (20 \times 10^{-3})^2 = 314.16 \times 10^{-6} \text{ m}^2$

Stress in rod  $AE$ :  $\sigma_{AE} = \frac{F_{AE}}{A} = \frac{4 \times 10^3}{314.16 \times 10^{-6}} = 12.7324 \times 10^6 \text{ Pa}$

(a)  $\sigma_{AE} = 12.73 \text{ MPa} \blacktriangleleft$

Use combined members  $ABC$  and  $BFD$  as free body.

$$+\curvearrowright \sum M_F = 0: (0.150) \left( \frac{4}{5} F_{AE} \right) - (0.200) \left( \frac{4}{5} F_{DG} \right) - (1.050 - 0.350)(800) = 0$$

$$F_{DG} = -1500 \text{ N}$$

Area of rod  $DG$ :  $A = \frac{\pi}{4} d^2 = \frac{\pi}{4} (20 \times 10^{-3})^2 = 314.16 \times 10^{-6} \text{ m}^2$

Stress in rod  $DG$ :  $\sigma_{DG} = \frac{F_{DG}}{A} = \frac{-1500}{3.1416 \times 10^{-6}} = -4.7746 \times 10^6 \text{ Pa}$

(b)  $\sigma_{DG} = -4.77 \text{ MPa} \blacktriangleleft$



Full file at <https://TestbankDirect.eu/>**PROBLEM 1.15**

Determine the diameter of the largest circular hole that can be punched into a sheet of polystyrene 6 mm thick, knowing that the force exerted by the punch is 45 kN and that a 55-MPa average shearing stress is required to cause the material to fail.

**SOLUTION**

For cylindrical failure surface:  $A = \pi dt$

Shearing stress:  $\tau = \frac{P}{A}$  or  $A = \frac{P}{\tau}$

Therefore,  $\frac{P}{\tau} = \pi dt$

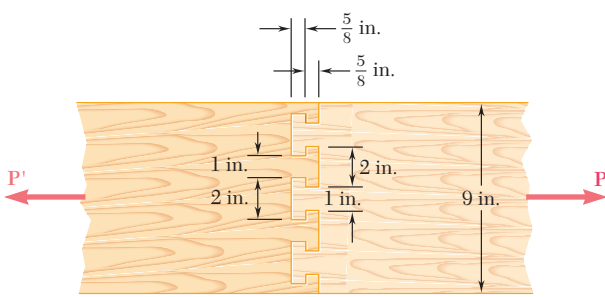
Finally,  $d = \frac{P}{\pi t \tau}$

$$\begin{aligned} &= \frac{45 \times 10^3 \text{ N}}{\pi(0.006 \text{ m})(55 \times 10^6 \text{ Pa})} \\ &= 43.406 \times 10^{-3} \text{ m} \end{aligned}$$

$$d = 43.4 \text{ mm} \blacktriangleleft$$

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**PROBLEM 1.16**

Two wooden planks, each  $\frac{1}{2}$  in. thick and 9 in. wide, are joined by the dry mortise joint shown. Knowing that the wood used shears off along its grain when the average shearing stress reaches 1.20 ksi, determine the magnitude  $P$  of the axial load that will cause the joint to fail.

**SOLUTION**

Six areas must be sheared off when the joint fails. Each of these areas has dimensions  $\frac{5}{8}$  in.  $\times$   $\frac{1}{2}$  in., its area being

$$A = \frac{5}{8} \times \frac{1}{2} = \frac{5}{16} \text{ in}^2 = 0.3125 \text{ in}^2$$

At failure, the force carried by each area is

$$F = \tau A = (1.20 \text{ ksi})(0.3125 \text{ in}^2) = 0.375 \text{ kips}$$

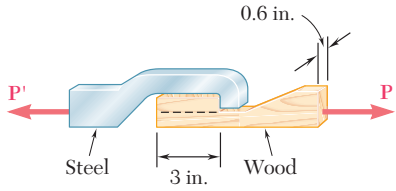
Since there are six failure areas,

$$P = 6F = (6)(0.375) \qquad P = 2.25 \text{ kips} \blacktriangleleft$$

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**PROBLEM 1.17**

When the force  $P$  reached 1600 lb, the wooden specimen shown failed in shear along the surface indicated by the dashed line. Determine the average shearing stress along that surface at the time of failure.

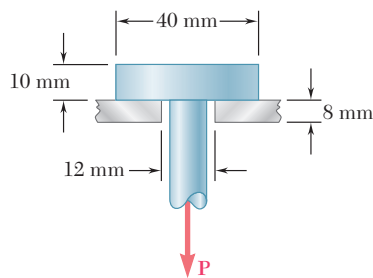
**SOLUTION**

Area being sheared:  $A = 3 \text{ in.} \times 0.6 \text{ in.} = 1.8 \text{ in}^2$

Force:  $P = 1600 \text{ lb}$

Shearing stress:  $\tau = \frac{P}{A} = \frac{1600 \text{ lb}}{1.8 \text{ in}^2} = 8.8889 \times 10^2 \text{ psi}$   $\tau = 889 \text{ psi} \blacktriangleleft$

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Full file at <https://TestbankDirect.eu/>**PROBLEM 1.18**

A load  $P$  is applied to a steel rod supported as shown by an aluminum plate into which a 12-mm-diameter hole has been drilled. Knowing that the shearing stress must not exceed 180 MPa in the steel rod and 70 MPa in the aluminum plate, determine the largest load  $P$  that can be applied to the rod.

**SOLUTION**

For steel:

$$A_1 = \pi dt = \pi(0.012 \text{ m})(0.010 \text{ m}) \\ = 376.99 \times 10^{-6} \text{ m}^2$$

$$\tau_1 = \frac{P}{A} \therefore P = A_1 \tau_1 = (376.99 \times 10^{-6} \text{ m}^2)(180 \times 10^6 \text{ Pa}) \\ = 67.858 \times 10^3 \text{ N}$$

For aluminum:

$$A_2 = \pi dt = \pi(0.040 \text{ m})(0.008 \text{ m}) = 1.00531 \times 10^{-3} \text{ m}^2$$

$$\tau_2 = \frac{P}{A_2} \therefore P = A_2 \tau_2 = (1.00531 \times 10^{-3} \text{ m}^2)(70 \times 10^6 \text{ Pa}) = 70.372 \times 10^3 \text{ N}$$

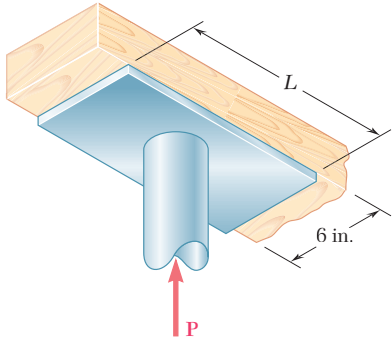
Limiting value of  $P$  is the smaller value, so

$$P = 67.9 \text{ kN} \blacktriangleleft$$

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**PROBLEM 1.19**

The axial force in the column supporting the timber beam shown is  $P = 20$  kips. Determine the smallest allowable length  $L$  of the bearing plate if the bearing stress in the timber is not to exceed 400 psi.

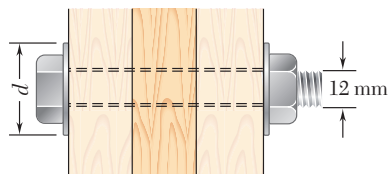
**SOLUTION**Bearing area:  $A_b = Lw$ 

$$\sigma_b = \frac{P}{A_b} = \frac{P}{Lw}$$

$$L = \frac{P}{\sigma_b w} = \frac{20 \times 10^3 \text{ lb}}{(400 \text{ psi})(6 \text{ in.})} = 8.33 \text{ in.}$$

$$L = 8.33 \text{ in.} \blacktriangleleft$$

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Full file at <https://TestbankDirect.eu/>**PROBLEM 1.20**

Three wooden planks are fastened together by a series of bolts to form a column. The diameter of each bolt is 12 mm and the inner diameter of each washer is 16 mm, which is slightly larger than the diameter of the holes in the planks. Determine the smallest allowable outer diameter  $d$  of the washers, knowing that the average normal stress in the bolts is 36 MPa and that the bearing stress between the washers and the planks must not exceed 8.5 MPa.

**SOLUTION**

Bolt: 
$$A_{\text{Bolt}} = \frac{\pi d^2}{4} = \frac{\pi(0.012 \text{ m})^2}{4} = 1.13097 \times 10^{-4} \text{ m}^2$$

Tensile force in bolt: 
$$\sigma = \frac{P}{A} \Rightarrow P = \sigma A$$

$$= (36 \times 10^6 \text{ Pa})(1.13097 \times 10^{-4} \text{ m}^2)$$

$$= 4.0715 \times 10^3 \text{ N}$$

Bearing area for washer: 
$$A_w = \frac{\pi}{4}(d_o^2 - d_i^2)$$

and 
$$A_w = \frac{P}{\sigma_{BRG}}$$

Therefore, equating the two expressions for  $A_w$  gives

$$\frac{\pi}{4}(d_o^2 - d_i^2) = \frac{P}{\sigma_{BRG}}$$

$$d_o^2 = \frac{4P}{\pi\sigma_{BRG}} + d_i^2$$

$$d_o^2 = \frac{4(4.0715 \times 10^3 \text{ N})}{\pi(8.5 \times 10^6 \text{ Pa})} + (0.016 \text{ m})^2$$

$$d_o^2 = 8.6588 \times 10^{-4} \text{ m}^2$$

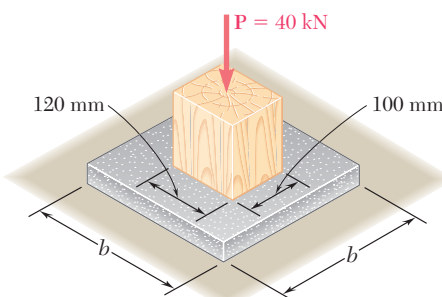
$$d_o = 29.426 \times 10^{-3} \text{ m}$$

$$d_o = 29.4 \text{ mm} \blacktriangleleft$$

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**PROBLEM 1.21**

A 40-kN axial load is applied to a short wooden post that is supported by a concrete footing resting on undisturbed soil. Determine (a) the maximum bearing stress on the concrete footing, (b) the size of the footing for which the average bearing stress in the soil is 145 kPa.

**SOLUTION**

- (a) Bearing stress on concrete footing.

$$P = 40 \text{ kN} = 40 \times 10^3 \text{ N}$$

$$A = (100)(120) = 12 \times 10^3 \text{ mm}^2 = 12 \times 10^{-3} \text{ m}^2$$

$$\sigma = \frac{P}{A} = \frac{40 \times 10^3}{12 \times 10^{-3}} = 3.3333 \times 10^6 \text{ Pa} \quad 3.33 \text{ MPa} \blacktriangleleft$$

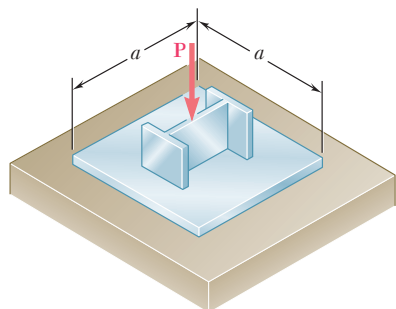
- (b) Footing area.
- $P = 40 \times 10^3 \text{ N}$
- $\sigma = 145 \text{ kPa} = 145 \times 10^3 \text{ Pa}$

$$\sigma = \frac{P}{A} \quad A = \frac{P}{\sigma} = \frac{40 \times 10^3}{145 \times 10^3} = 0.27586 \text{ m}^2$$

Since the area is square,  $A = b^2$ 

$$b = \sqrt{A} = \sqrt{0.27586} = 0.525 \text{ m} \quad b = 525 \text{ mm} \blacktriangleleft$$

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Full file at <https://TestbankDirect.eu/>**PROBLEM 1.22**

An axial load  $P$  is supported by a short  $W8 \times 40$  column of cross-sectional area  $A = 11.7 \text{ in}^2$  and is distributed to a concrete foundation by a square plate as shown. Knowing that the average normal stress in the column must not exceed 30 ksi and that the bearing stress on the concrete foundation must not exceed 3.0 ksi, determine the side  $a$  of the plate that will provide the most economical and safe design.

**SOLUTION**

For the column,  $\sigma = \frac{P}{A}$  or

$$P = \sigma A = (30)(11.7) = 351 \text{ kips}$$

For the  $a \times a$  plate,  $\sigma = 3.0 \text{ ksi}$

$$A = \frac{P}{\sigma} = \frac{351}{3.0} = 117 \text{ in}^2$$

Since the plate is square,  $A = a^2$

$$a = \sqrt{A} = \sqrt{117}$$

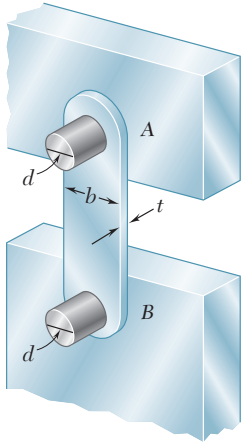
$$a = 10.82 \text{ in.} \quad \blacktriangleleft$$

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**PROBLEM 1.23**

Link AB, of width  $b = 2$  in. and thickness  $t = \frac{1}{4}$  in., is used to support the end of a horizontal beam. Knowing that the average normal stress in the link is  $-20$  ksi and that the average shearing stress in each of the two pins is  $12$  ksi, determine (a) the diameter  $d$  of the pins, (b) the average bearing stress in the link.

**SOLUTION**Rod  $AB$  is in compression.

$$A = bt \quad \text{where } b = 2 \text{ in. and } t = \frac{1}{4} \text{ in.}$$

$$P = -\sigma A = -(-20)(2)\left(\frac{1}{4}\right) = 10 \text{ kips}$$

Pin: 
$$\tau_P = \frac{P}{A_P}$$

and 
$$A_P = \frac{\pi}{4}d^2$$

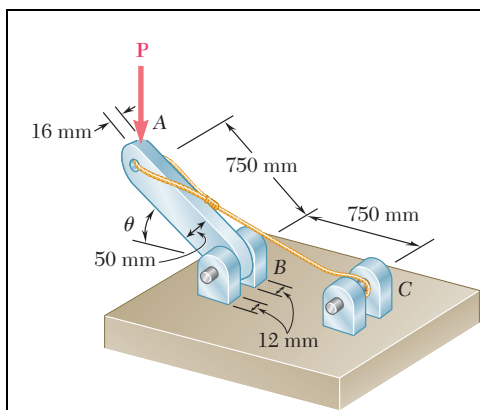
$$(a) \quad d = \sqrt{\frac{4A_P}{\pi}} = \sqrt{\frac{4P}{\pi\tau_P}} = \sqrt{\frac{(4)(10)}{\pi(12)}} = 1.03006 \text{ in.}$$

$$d = 1.030 \text{ in.} \blacktriangleleft$$

$$(b) \quad \sigma_b = \frac{P}{dt} = \frac{10}{(1.03006)(0.25)} = 38.833 \text{ ksi}$$

$$\sigma_b = 38.8 \text{ ksi} \blacktriangleleft$$

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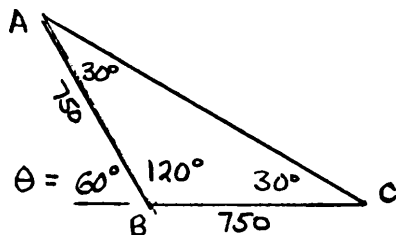


### PROBLEM 1.24

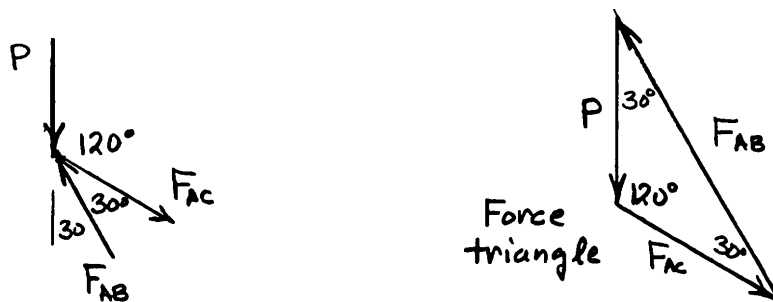
Determine the largest load  $P$  which may be applied at  $A$  when  $\theta = 60^\circ$ , knowing that the average shearing stress in the 10-mm-diameter pin at  $B$  must not exceed 120 MPa and that the average bearing stress in member  $AB$  and in the bracket at  $B$  must not exceed 90 MPa.

### SOLUTION

Geometry: Triangle  $ABC$  is an isosceles triangle with angles shown here.



Use joint  $A$  as a free body.



Law of sines applied to force triangle:

$$\frac{P}{\sin 30^\circ} = \frac{F_{AB}}{\sin 120^\circ} = \frac{F_{AC}}{\sin 30^\circ}$$

$$P = \frac{F_{AB} \sin 30^\circ}{\sin 120^\circ} = 0.57735 F_{AB}$$

$$P = \frac{F_{AC} \sin 30^\circ}{\sin 30^\circ} = F_{AC}$$

Full file at <https://TestbankDirect.eu/>**PROBLEM 1.24 (Continued)**If shearing stress in pin at  $B$  is critical,

$$A = \frac{\pi}{4}d^2 = \frac{\pi}{4}(0.010)^2 = 78.54 \times 10^{-6} \text{ m}^2$$

$$F_{AB} = 2A\tau = (2)(78.54 \times 10^{-6})(120 \times 10^6) = 18.850 \times 10^3 \text{ N}$$

If bearing stress in member  $AB$  at bracket at  $A$  is critical,

$$A_b = td = (0.016)(0.010) = 160 \times 10^{-6} \text{ m}^2$$

$$F_{AB} = A_b\sigma_b = (160 \times 10^{-6})(90 \times 10^6) = 14.40 \times 10^3 \text{ N}$$

If bearing stress in the bracket at  $B$  is critical,

$$A_b = 2td = (2)(0.012)(0.010) = 240 \times 10^{-6} \text{ m}^2$$

$$F_{AB} = A_b\sigma_b = (240 \times 10^{-6})(90 \times 10^6) = 21.6 \times 10^3 \text{ N}$$

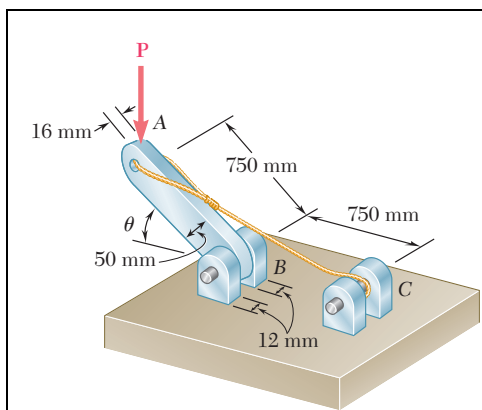
Allowable  $F_{AB}$  is the smallest, i.e.,  $14.40 \times 10^3 \text{ N}$ 

Then from statics,

$$\begin{aligned} P_{\text{allow}} &= (0.57735)(14.40 \times 10^3) \\ &= 8.31 \times 10^3 \text{ N} \end{aligned}$$

8.31 kN ◀

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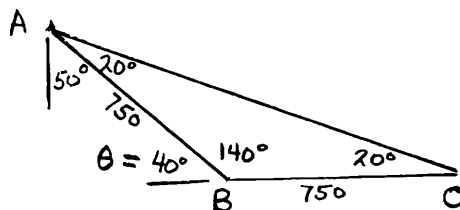


### PROBLEM 1.25

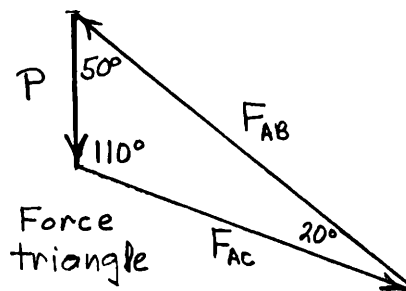
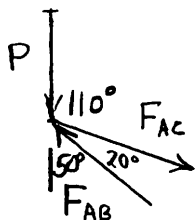
Knowing that  $\theta = 40^\circ$  and  $P = 9$  kN, determine (a) the smallest allowable diameter of the pin at  $B$  if the average shearing stress in the pin is not to exceed 120 MPa, (b) the corresponding average bearing stress in member  $AB$  at  $B$ , (c) the corresponding average bearing stress in each of the support brackets at  $B$ .

### SOLUTION

Geometry: Triangle  $ABC$  is an isosceles triangle with angles shown here.



Use joint  $A$  as a free body.



Law of sines applied to force triangle:

$$\begin{aligned} \frac{P}{\sin 20^\circ} &= \frac{F_{AB}}{\sin 110^\circ} = \frac{F_{AC}}{\sin 50^\circ} \\ F_{AB} &= \frac{P \sin 110^\circ}{\sin 20^\circ} \\ &= \frac{(9) \sin 110^\circ}{\sin 20^\circ} = 24.727 \text{ kN} \end{aligned}$$

**PROBLEM 1.25 (Continued)**(a) Allowable pin diameter.

$$\tau = \frac{F_{AB}}{2A_p} = \frac{F_{AB}}{2\frac{\pi}{4}d^2} = \frac{2F_{AB}}{\pi d^2} \text{ where } F_{AB} = 24.727 \times 10^3 \text{ N}$$

$$d^2 = \frac{2F_{AB}}{\pi\tau} = \frac{(2)(24.727 \times 10^3)}{\pi(120 \times 10^6)} = 131.181 \times 10^{-6} \text{ m}^2$$

$$d = 11.4534 \times 10^{-3} \text{ m} \quad 11.45 \text{ mm} \blacktriangleleft$$

(b) Bearing stress in AB at A.

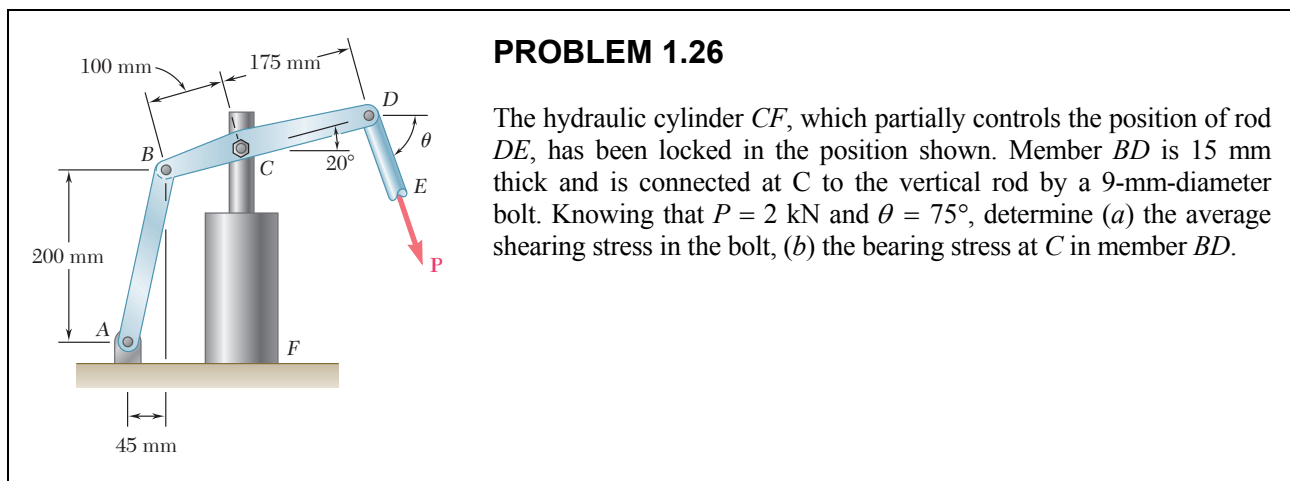
$$A_b = td = (0.016)(11.4534 \times 10^{-3}) = 183.254 \times 10^{-6} \text{ m}^2$$

$$\sigma_b = \frac{F_{AB}}{A_b} = \frac{24.727 \times 10^3}{183.254 \times 10^{-6}} = 134.933 \times 10^6 \text{ Pa} \quad 134.9 \text{ MPa} \blacktriangleleft$$

(c) Bearing stress in support brackets at B.

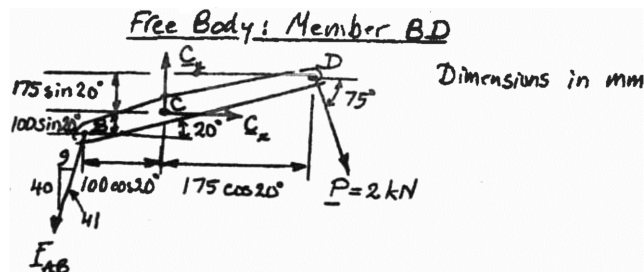
$$A = td = (0.012)(11.4534 \times 10^{-3}) = 137.441 \times 10^{-6} \text{ m}^2$$

$$\sigma_b = \frac{\frac{1}{2}F_{AB}}{A} = \frac{(0.5)(24.727 \times 10^3)}{137.441 \times 10^{-6}} = 89.955 \times 10^6 \text{ Pa} \quad 90.0 \text{ MPa} \blacktriangleleft$$



**SOLUTION**

Free Body: Member  $BD$ .



$$\begin{aligned}
 +\sum M_C = 0: & \quad \frac{40}{41}F_{AB}(100 \cos 20^\circ) - \frac{9}{4}F_{AB}(100 \sin 20^\circ) \\
 & \quad - (2 \text{ kN}) \cos 75^\circ(175 \sin 20^\circ) - (2 \text{ kN}) \sin 75^\circ(175 \cos 20^\circ) = 0 \\
 \frac{100}{41}F_{AB}(40 \cos 20^\circ - 9 \sin 20^\circ) & = (2 \text{ kN})(175) \sin(75^\circ + 20^\circ) \\
 F_{AB} & = 4.1424 \text{ kN}
 \end{aligned}$$

$$\begin{aligned}
 +\sum F_x = 0: & \quad C_x - \frac{9}{41}(4.1424 \text{ kN}) + (2 \text{ kN}) \cos 75^\circ = 0 \\
 C_x & = 0.39167 \text{ kN}
 \end{aligned}$$

$$\begin{aligned}
 +\sum F_y = 0: & \quad C_y - \frac{40}{41}(4.1424 \text{ kN}) - (2 \text{ kN}) \sin 75^\circ = 0 \\
 C_y & = 5.9732 \text{ kN} \\
 C & = 5.9860 \text{ kN} \angle 86.2^\circ
 \end{aligned}$$

(a)  $\tau_{\text{ave}} = \frac{C}{A} = \frac{5.9860 \times 10^3 \text{ N}}{\pi(0.0045 \text{ m})^2} = 94.1 \times 10^6 \text{ Pa} = 94.1 \text{ MPa}$  ◀

(b)  $\tau_b = \frac{C}{td} = \frac{5.9860 \times 10^3 \text{ N}}{(0.015 \text{ m})(0.009 \text{ m})} = 44.3 \times 10^6 \text{ Pa} = 44.3 \text{ MPa}$  ◀

**PROBLEM 1.27**

For the assembly and loading of Prob. 1.7, determine (a) the average shearing stress in the pin at B, (b) the average bearing stress at B in member BD, (c) the average bearing stress at B in member ABC, knowing that this member has a  $10 \times 50$ -mm uniform rectangular cross section.

**PROBLEM 1.7** Each of the four vertical links has an  $8 \times 36$ -mm uniform rectangular cross section and each of the four pins has a 16-mm diameter. Determine the maximum value of the average normal stress in the links connecting (a) points B and D, (b) points C and E.

**SOLUTION**

Use bar *ABC* as a free body.

$$\overset{+}{\curvearrowright} \Sigma M_C = 0 : (0.040)F_{BD} - (0.025 + 0.040)(20 \times 10^3) = 0$$

$$F_{BD} = 32.5 \times 10^3 \text{ N}$$

(a) Shear pin at B.  $\tau = \frac{F_{BD}}{2A}$  for double shear

where  $A = \frac{\pi}{4}d^2 = \frac{\pi}{4}(0.016)^2 = 201.06 \times 10^{-6} \text{ m}^2$

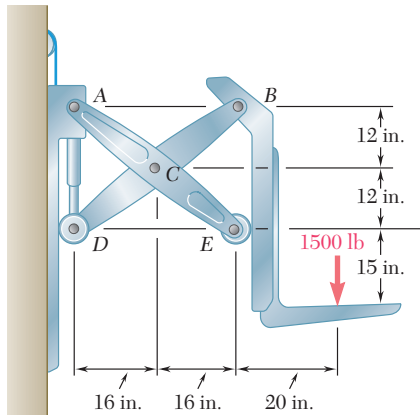
$$\tau = \frac{32.5 \times 10^3}{(2)(201.06 \times 10^{-6})} = 80.822 \times 10^6 \text{ Pa} \quad \tau = 80.8 \text{ MPa} \quad \blacktriangleleft$$

(b) Bearing: link BD.  $A = dt = (0.016)(0.008) = 128 \times 10^{-6} \text{ m}^2$

$$\sigma_b = \frac{\frac{1}{2}F_{BD}}{A} = \frac{(0.5)(32.5 \times 10^3)}{128 \times 10^{-6}} = 126.95 \times 10^6 \text{ Pa} \quad \sigma_b = 127.0 \text{ MPa} \quad \blacktriangleleft$$

(c) Bearing in ABC at B.  $A = dt = (0.016)(0.010) = 160 \times 10^{-6} \text{ m}^2$

$$\sigma_b = \frac{F_{BD}}{A} = \frac{32.5 \times 10^3}{160 \times 10^{-6}} = 203.12 \times 10^6 \text{ Pa} \quad \sigma_b = 203 \text{ MPa} \quad \blacktriangleleft$$

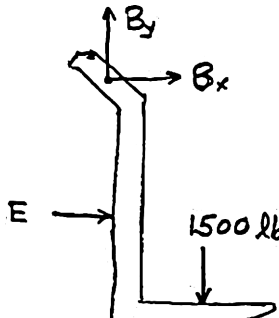


### PROBLEM 1.28

Two identical linkage-and-hydraulic-cylinder systems control the position of the forks of a fork-lift truck. The load supported by the one system shown is 1500 lb. Knowing that the thickness of member  $BD$  is  $\frac{5}{8}$  in., determine (a) the average shearing stress in the  $\frac{1}{2}$ -in.-diameter pin at  $B$ , (b) the bearing stress at  $B$  in member  $BD$ .

### SOLUTION

Use one fork as a free body.



$$+\curvearrowright \Sigma M_B = 0: 24E - (20)(1500) = 0$$

$$E = 1250 \text{ lb} \rightarrow$$

$$+\rightarrow \Sigma F_x = 0: E + B_x = 0$$

$$B_x = -E$$

$$B_x = 1250 \text{ lb} \leftarrow$$

$$+\uparrow \Sigma F_y = 0: B_y - 1500 = 0 \quad B_y = 1500 \text{ lb}$$

$$B = \sqrt{B_x^2 + B_y^2} = \sqrt{1250^2 + 1500^2} = 1952.56 \text{ lb}$$

(a) Shearing stress in pin at  $B$ .

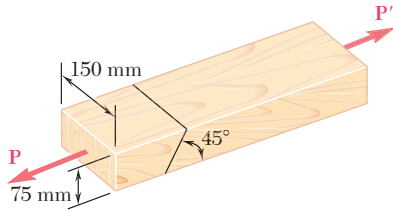
$$A_{\text{pin}} = \frac{\pi}{4} d_{\text{pin}}^2 = \frac{\pi}{4} \left(\frac{1}{2}\right)^2 = 0.196350 \text{ in}^2$$

$$\tau = \frac{B}{A_{\text{pin}}} = \frac{1952.56}{0.196350} = 9.94 \times 10^3 \text{ psi} \quad \tau = 9.94 \text{ ksi} \blacktriangleleft$$

(b) Bearing stress at  $B$ .

$$\sigma = \frac{B}{dt} = \frac{1952.56}{\left(\frac{1}{2}\right)\left(\frac{5}{8}\right)} = 6.25 \times 10^3 \text{ psi} \quad \sigma = 6.25 \text{ ksi} \blacktriangleleft$$



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**PROBLEM 1.29**

Two wooden members of uniform rectangular cross section are joined by the simple glued scarf splice shown. Knowing that  $P = 11$  kN, determine the normal and shearing stresses in the glued splice.

**SOLUTION**

$$\theta = 90^\circ - 45^\circ = 45^\circ$$

$$P = 11 \text{ kN} = 11 \times 10^3 \text{ N}$$

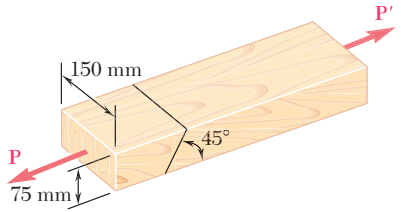
$$A_0 = (150)(75) = 11.25 \times 10^3 \text{ mm}^2 = 11.25 \times 10^{-3} \text{ m}^2$$

$$\sigma = \frac{P \cos^2 \theta}{A_0} = \frac{(11 \times 10^3) \cos^2 45^\circ}{11.25 \times 10^{-3}} = 489 \times 10^3 \text{ Pa} \quad \sigma = 489 \text{ kPa} \quad \blacktriangleleft$$

$$\tau = \frac{P \sin 2\theta}{2A_0} = \frac{(11 \times 10^3)(\sin 90^\circ)}{(2)(11.25 \times 10^{-3})} = 489 \times 10^3 \text{ Pa} \quad \tau = 489 \text{ kPa} \quad \blacktriangleleft$$

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### PROBLEM 1.30

Two wooden members of uniform rectangular cross section are joined by the simple glued scarf splice shown. Knowing that the maximum allowable shearing stress in the glued splice is 620 kPa, determine (a) the largest load **P** that can be safely applied, (b) the corresponding tensile stress in the splice.

**SOLUTION**

$$\theta = 90^\circ - 45^\circ = 45^\circ$$

$$A_0 = (150)(75) = 11.25 \times 10^3 \text{ mm}^2 = 11.25 \times 10^{-3} \text{ m}^2$$

$$\tau = 620 \text{ kPa} = 620 \times 10^3 \text{ Pa}$$

$$\tau = \frac{P \sin 2\theta}{2A_0}$$

$$(a) \quad P = \frac{2A_0\tau}{\sin 2\theta} = \frac{(2)(11.25 \times 10^{-3})(620 \times 10^3)}{\sin 90^\circ}$$

$$= 13.95 \times 10^3 \text{ N}$$

$$P = 13.95 \text{ kN} \quad \blacktriangleleft$$

$$(b) \quad \sigma = \frac{P \cos^2 \theta}{A_0} = \frac{(13.95 \times 10^3)(\cos 45^\circ)^2}{11.25 \times 10^{-3}}$$

$$= 620 \times 10^3 \text{ Pa}$$

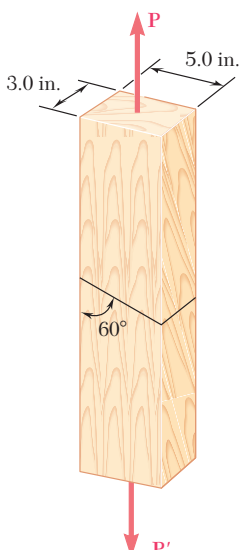
$$\sigma = 620 \text{ kPa} \quad \blacktriangleleft$$

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**PROBLEM 1.31**

The 1.4-kip load  $P$  is supported by two wooden members of uniform cross section that are joined by the simple glued scarf splice shown. Determine the normal and shearing stresses in the glued splice.

**SOLUTION**

$$P = 1400 \text{ lb} \quad \theta = 90^\circ - 60^\circ = 30^\circ$$

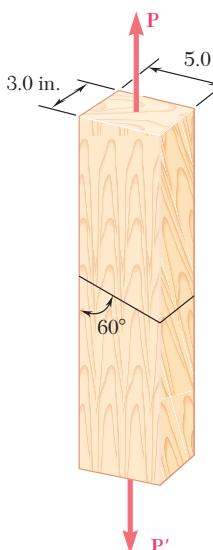
$$A_0 = (5.0)(3.0) = 15 \text{ in}^2$$

$$\sigma = \frac{P \cos^2 \theta}{A_0} = \frac{(1400)(\cos 30^\circ)^2}{15} \quad \sigma = 70.0 \text{ psi} \quad \blacktriangleleft$$

$$\tau = \frac{P \sin 2\theta}{2A_0} = \frac{(1400)\sin 60^\circ}{(2)(15)} \quad \tau = 40.4 \text{ psi} \quad \blacktriangleleft$$

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**PROBLEM 1.32**

Two wooden members of uniform cross section are joined by the simple scarf splice shown. Knowing that the maximum allowable tensile stress in the glued splice is 75 psi, determine (a) the largest load **P** that can be safely supported, (b) the corresponding shearing stress in the splice.

**SOLUTION**

$$A_0 = (5.0)(3.0) = 15 \text{ in}^2$$

$$\theta = 90^\circ - 60^\circ = 30^\circ$$

$$\sigma = \frac{P \cos^2 \theta}{A_0}$$

$$(a) \quad P = \frac{\sigma A_0}{\cos^2 \theta} = \frac{(75)(15)}{\cos^2 30^\circ} = 1500 \text{ lb} \quad P = 1.500 \text{ kips} \blacktriangleleft$$

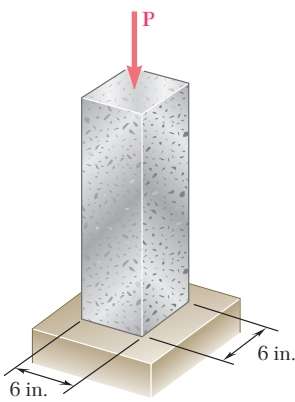
$$(b) \quad \tau = \frac{P \sin 2\theta}{2A_0} = \frac{(1500) \sin 60^\circ}{(2)(15)} \quad \tau = 43.3 \text{ psi} \blacktriangleleft$$

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**PROBLEM 1.33**

A centric load  $\mathbf{P}$  is applied to the granite block shown. Knowing that the resulting maximum value of the shearing stress in the block is 2.5 ksi, determine (a) the magnitude of  $\mathbf{P}$ , (b) the orientation of the surface on which the maximum shearing stress occurs, (c) the normal stress exerted on that surface, (d) the maximum value of the normal stress in the block.

**SOLUTION**

$$A_0 = (6)(6) = 36 \text{ in}^2$$

$$\tau_{\max} = 2.5 \text{ ksi}$$

$$\theta = 45^\circ \text{ for plane of } \tau_{\max}$$

$$(a) \quad \tau_{\max} = \frac{|P|}{2A_0} \quad \therefore |P| = 2A_0\tau_{\max} = (2)(36)(2.5) \quad P = 180.0 \text{ kips} \blacktriangleleft$$

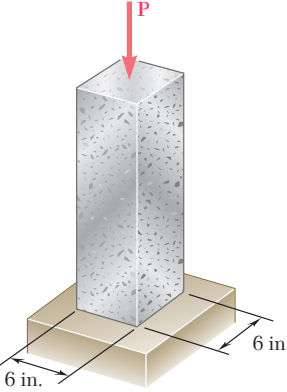
$$(b) \quad \sin 2\theta = 1 \quad 2\theta = 90^\circ \quad \theta = 45.0^\circ \blacktriangleleft$$

$$(c) \quad \sigma_{45} = \frac{P}{A_0} \cos^2 45^\circ = \frac{P}{2A_0} = -\frac{180}{(2)(36)} \quad \sigma_{45} = -2.50 \text{ ksi} \blacktriangleleft$$

$$(d) \quad \sigma_{\max} = \frac{P}{A_0} = \frac{-180}{36} \quad \sigma_{\max} = -5.00 \text{ ksi} \blacktriangleleft$$

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**PROBLEM 1.34**

A 240-kip load  $P$  is applied to the granite block shown. Determine the resulting maximum value of (a) the normal stress, (b) the shearing stress. Specify the orientation of the plane on which each of these maximum values occurs.

**SOLUTION**

$$A_0 = (6)(6) = 36 \text{ in}^2$$

$$\sigma = \frac{P}{A_0} \cos^2 \theta = \frac{-240}{36} \cos^2 \theta = -6.67 \cos^2 \theta$$

(a) max tensile stress = 0 at  $\theta = 90.0^\circ$   
 max. compressive stress = 6.67 ksi at  $\theta = 0^\circ$  ◀

(b)  $\tau_{\max} = \frac{P}{2A_0} = \frac{240}{(2)(36)}$

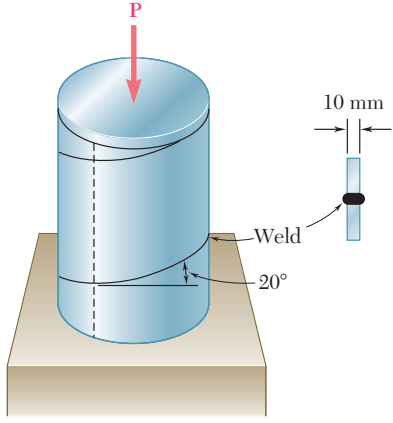
$\tau_{\max} = 3.33 \text{ ksi}$  ◀  
 at  $\theta = 45^\circ$

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The diagram shows a blue cylindrical steel pipe resting on a brown base. A red arrow labeled 'P' points downwards from the top center of the pipe. A dashed vertical line represents the pipe's axis. A weld is shown as a black line spiraling around the pipe. A callout shows a cross-section of the pipe wall, which is 10 mm thick. The weld line is at an angle of 20 degrees to the vertical axis.

**PROBLEM 1.35**

A steel pipe of 400-mm outer diameter is fabricated from 10-mm thick plate by welding along a helix that forms an angle of  $20^\circ$  with a plane perpendicular to the axis of the pipe. Knowing that a 300-kN axial force  $\mathbf{P}$  is applied to the pipe, determine the normal and shearing stresses in directions respectively normal and tangential to the weld.

**SOLUTION**

$$d_o = 0.400 \text{ m}$$

$$r_o = \frac{1}{2}d_o = 0.200 \text{ m}$$

$$r_i = r_o - t = 0.200 - 0.010 = 0.190 \text{ m}$$

$$A_o = \pi(r_o^2 - r_i^2) = \pi(0.200^2 - 0.190^2)$$

$$= 12.2522 \times 10^{-3} \text{ m}^2$$

$$\theta = 20^\circ$$

$$\sigma = \frac{P}{A_o} = \cos^2 \theta = \frac{-300 \times 10^3 \cos^2 20^\circ}{12.2522 \times 10^{-3}} = 21.621 \times 10^6 \text{ Pa} \quad \sigma = -21.6 \text{ MPa} \blacktriangleleft$$

$$\tau = \frac{P}{2A_o} = \sin 2\theta = \frac{-300 \times 10^3 \sin 40^\circ}{(2)(12.2522 \times 10^{-3})} = 7.8695 \times 10^6 \text{ Pa} \quad \tau = 7.87 \text{ MPa} \blacktriangleleft$$

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**PROBLEM 1.36**

A steel pipe of 400-mm outer diameter is fabricated from 10-mm thick plate by welding along a helix that forms an angle of  $20^\circ$  with a plane perpendicular to the axis of the pipe. Knowing that the maximum allowable normal and shearing stresses in the directions respectively normal and tangential to the weld are  $\sigma = 60$  MPa and  $\tau = 36$  MPa, determine the magnitude  $P$  of the largest axial force that can be applied to the pipe.

**SOLUTION**

$$d_o = 0.400 \text{ m}$$

$$r_o = \frac{1}{2}d_o = 0.200 \text{ m}$$

$$r_i = r_o - t = 0.200 - 0.010 = 0.190 \text{ m}$$

$$A_o = \pi(r_o^2 - r_i^2) = \pi(0.200^2 - 0.190^2)$$

$$= 12.2522 \times 10^{-3} \text{ m}^2$$

$$\theta = 20^\circ$$

Based on  $|\sigma| = 60$  MPa:  $\sigma = \frac{P}{A_o} \cos^2 \theta$

$$P = \frac{A_o \sigma}{\cos^2 \theta} = \frac{(12.2522 \times 10^{-3})(60 \times 10^6)}{\cos^2 20^\circ} = 832.52 \times 10^3 \text{ N}$$

Based on  $|\tau| = 30$  MPa:  $\tau = \frac{P}{2A_o} \sin 2\theta$

$$P = \frac{2A_o \tau}{\sin 2\theta} = \frac{(2)(12.2522 \times 10^{-3})(36 \times 10^6)}{\sin 40^\circ} = 1372.39 \times 10^3 \text{ N}$$

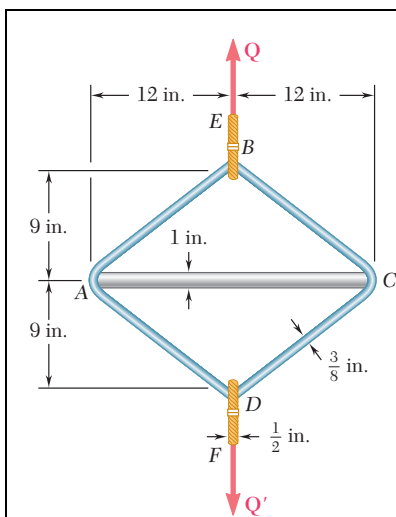
Smaller value is the allowable value of  $P$ .

$$P = 833 \text{ kN} \blacktriangleleft$$

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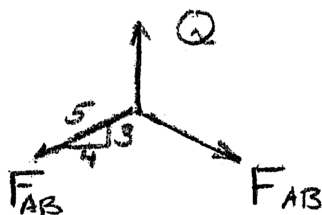




### PROBLEM 1.37

A steel loop  $ABCD$  of length 5 ft and of  $\frac{3}{8}$ -in. diameter is placed as shown around a 1-in.-diameter aluminum rod  $AC$ . Cables  $BE$  and  $DF$ , each of  $\frac{1}{2}$ -in. diameter, are used to apply the load  $Q$ . Knowing that the ultimate strength of the steel used for the loop and the cables is 70 ksi, and that the ultimate strength of the aluminum used for the rod is 38 ksi, determine the largest load  $Q$  that can be applied if an overall factor of safety of 3 is desired.

### SOLUTION



Using joint  $B$  as a free body and considering symmetry,

$$2 \cdot \frac{3}{5} F_{AB} - Q = 0 \quad Q = \frac{6}{5} F_{AB}$$

Using joint  $A$  as a free body and considering symmetry,

$$2 \cdot \frac{4}{5} F_{AB} - F_{AC} = 0$$

$$\frac{8}{5} \cdot \frac{5}{6} Q - F_{AC} = 0 \quad \therefore Q = \frac{3}{4} F_{AC}$$

Based on strength of cable  $BE$ ,

$$Q_U = \sigma_U A = \sigma_U \frac{\pi}{4} d^2 = (70) \frac{\pi}{4} \left( \frac{1}{2} \right)^2 = 13.7445 \text{ kips}$$

Based on strength of steel loop,

$$\begin{aligned} Q_U &= \frac{6}{5} F_{AB,U} = \frac{6}{5} \sigma_U A = \frac{6}{5} \sigma_U \frac{\pi}{4} d^2 \\ &= \frac{6}{5} (70) \frac{\pi}{4} \left( \frac{3}{8} \right)^2 = 9.2775 \text{ kips} \end{aligned}$$

Based on strength of rod  $AC$ ,

$$Q_U = \frac{3}{4} F_{AC,U} = \frac{3}{4} \sigma_U A = \frac{3}{4} \sigma_U \frac{\pi}{4} d^2 = \frac{3}{4} (38) \frac{\pi}{4} (1.0)^2 = 22.384 \text{ kips}$$

Actual ultimate load  $Q_U$  is the smallest,  $\therefore Q_U = 9.2775 \text{ kips}$

Allowable load:

$$Q = \frac{Q_U}{F.S.} = \frac{9.2775}{3} = 3.0925 \text{ kips}$$

$Q = 3.09 \text{ kips} \blacktriangleleft$

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**PROBLEM 1.38**

Link  $BC$  is 6 mm thick, has a width  $w = 25$  mm, and is made of a steel with a 480-MPa ultimate strength in tension. What was the safety factor used if the structure shown was designed to support a 16-kN load  $P$ ?

**SOLUTION**

Use bar  $ACD$  as a free body and note that member  $BC$  is a two-force member.

$$\Sigma M_A = 0:$$

$$(480)F_{BC} - (600)P = 0$$

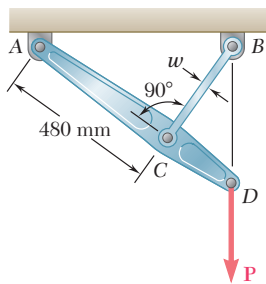
$$F_{BC} = \frac{600}{480}P = \frac{(600)(16 \times 10^3)}{480} = 20 \times 10^3 \text{ N}$$

Ultimate load for member  $BC$ :  $F_U = \sigma_U A$

$$F_U = (480 \times 10^6)(0.006)(0.025) = 72 \times 10^3 \text{ N}$$

Factor of safety:  $F.S. = \frac{F_U}{F_{BC}} = \frac{72 \times 10^3}{20 \times 10^3} \qquad F.S. = 3.60 \blacktriangleleft$

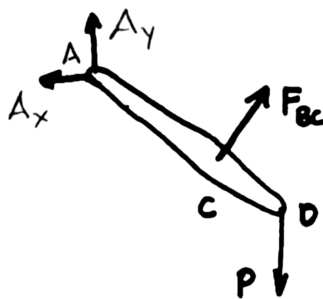
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Full file at <https://TestbankDirect.eu/>**PROBLEM 1.39**

Link  $BC$  is 6 mm thick and is made of a steel with a 450-MPa ultimate strength in tension. What should be its width  $w$  if the structure shown is being designed to support a 20-kN load  $P$  with a factor of safety of 3?

**SOLUTION**

Use bar  $ACD$  as a free body and note that member  $BC$  is a two-force member.



$$\Sigma M_A = 0:$$

$$(480)F_{BC} - 600P = 0$$

$$F_{BC} = \frac{600P}{480} = \frac{(600)(20 \times 10^3)}{480} = 25 \times 10^3 \text{ N}$$

For a factor of safety F.S. = 3, the ultimate load of member  $BC$  is

$$F_U = (\text{F.S.})(F_{BC}) = (3)(25 \times 10^3) = 75 \times 10^3 \text{ N}$$

$$\text{But } F_U = \sigma_U A \quad \therefore \quad A = \frac{F_U}{\sigma_U} = \frac{75 \times 10^3}{450 \times 10^6} = 166.667 \times 10^{-6} \text{ m}^2$$

$$\text{For a rectangular section, } A = wt \text{ or } w = \frac{A}{t} = \frac{166.667 \times 10^{-6}}{0.006} = 27.778 \times 10^{-3} \text{ m}$$

$$w = 27.8 \text{ mm} \quad \blacktriangleleft$$

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**PROBLEM 1.40**

Members  $AB$  and  $BC$  of the truss shown are made of the same alloy. It is known that a 20-mm-square bar of the same alloy was tested to failure and that an ultimate load of 120 kN was recorded. If a factor of safety of 3.2 is to be achieved for both bars, determine the required cross-sectional area of (a) bar  $AB$ , (b) bar  $AC$ .

**SOLUTION**

Length of member  $AB$ :

$$\ell_{AB} = \sqrt{0.75^2 + 0.4^2} = 0.85 \text{ m}$$

Use entire truss as a free body.

$$+\curvearrowright \Sigma M_c = 0: 1.4A_y - (0.75)(28) = 0$$

$$A_x = 15 \text{ kN}$$

$$+\uparrow \Sigma F_y = 0: A_y - 28 = 0$$

$$A_y = 28 \text{ kN}$$

Use Joint  $A$  as free body.

$$\pm \rightarrow \Sigma F_x = 0: \frac{0.75}{0.85} F_{AB} - A_x = 0$$

$$F_{AB} = \frac{(0.85)(15)}{0.75} = 17 \text{ kN}$$

$$+\uparrow \Sigma F_y = 0: A_y - F_{AC} - \frac{0.4}{0.85} F_{AB} = 0$$

$$F_{AC} = 28 - \frac{(0.4)(17)}{0.85} = 20 \text{ kN}$$

For the test bar,

$$A = (0.020)^2 = 400 \times 10^{-6} \text{ m}^2 \quad P_U = 120 \times 10^3 \text{ N}$$

For the material,

$$\sigma_U = \frac{P_U}{A} = \frac{120 \times 10^3}{400 \times 10^{-6}} = 300 \times 10^6 \text{ Pa}$$

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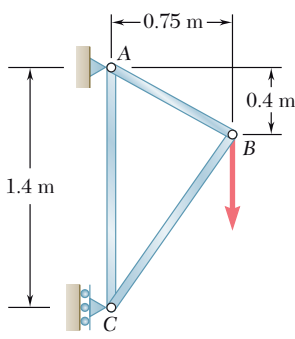
**PROBLEM 1.40 (Continued)**

(a) For member  $AB$ : 
$$\text{F.S.} = \frac{P_U}{F_{AB}} = \frac{\sigma_U A_{AB}}{F_{AB}}$$

$$A_{AB} = \frac{(\text{F.S.})F_{AB}}{\sigma_U} = \frac{(3.2)(17 \times 10^3)}{300 \times 10^6} = 181.333 \times 10^{-6} \text{ m}^2 \quad A_{AB} = 181.3 \text{ mm}^2 \blacktriangleleft$$

(b) For member  $AC$ : 
$$\text{F.S.} = \frac{P_U}{F_{AC}} = \frac{\sigma_U A_{AC}}{F_{AC}}$$

$$A_{AC} = \frac{(\text{F.S.})F_{AC}}{\sigma_U} = \frac{(3.2)(20 \times 10^3)}{300 \times 10^6} = 213.33 \times 10^{-6} \text{ m}^2 \quad A_{AC} = 213 \text{ mm}^2 \blacktriangleleft$$



**PROBLEM 1.41**

Members  $AB$  and  $BC$  of the truss shown are made of the same alloy. It is known that a 20-mm-square bar of the same alloy was tested to failure and that an ultimate load of 120 kN was recorded. If bar  $AB$  has a cross-sectional area of  $225 \text{ mm}^2$ , determine (a) the factor of safety for bar  $AB$  and (b) the cross-sectional area of bar  $AC$  if it is to have the same factor of safety as bar  $AB$ .

**SOLUTION**

Length of member  $AB$ :

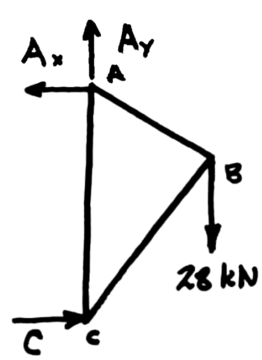
$$\ell_{AB} = \sqrt{0.75^2 + 0.4^2} = 0.85 \text{ m}$$

Use entire truss as a free body.

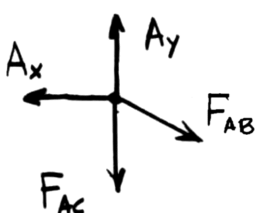
$$+\curvearrowright \sum M_c = 0: 1.4A_x - (0.75)(28) = 0$$

$$A_x = 15 \text{ kN}$$

$$+\uparrow \sum F_y = 0: A_y - 28 = 0$$

$$A_y = 28 \text{ kN}$$


Use Joint  $A$  as free body.



$$+\rightarrow \sum F_x = 0: \frac{0.75}{0.85} F_{AB} - A_x = 0$$

$$F_{AB} = \frac{(0.85)(15)}{0.75} = 17 \text{ kN}$$

$$+\uparrow \sum F_y = 0: A_y - F_{AC} - \frac{0.4}{0.85} F_{AB} = 0$$

$$F_{AC} = 28 - \frac{(0.4)(17)}{0.85} = 20 \text{ kN}$$

For the test bar,

$$A = (0.020)^2 = 400 \times 10^{-6} \text{ m}^2 \quad P_U = 120 \times 10^3 \text{ N}$$

For the material,

$$\sigma_U = \frac{P_U}{A} = \frac{120 \times 10^3}{400 \times 10^{-6}} = 300 \times 10^6 \text{ Pa}$$

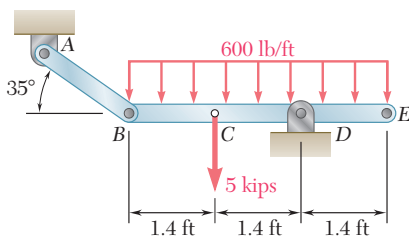
**PROBLEM 1.41 (Continued)**

(a) For bar  $AB$ : 
$$\text{F.S.} = \frac{F_U}{F_{AB}} = \frac{\sigma_U A_{AB}}{F_{AB}} = \frac{(300 \times 10^6)(225 \times 10^{-6})}{17 \times 10^3}$$

F.S. = 3.97 ◀

(b) For bar  $AC$ : 
$$\text{F.S.} = \frac{F_U}{F_{AC}} = \frac{\sigma_U A_{AC}}{F_{AC}}$$

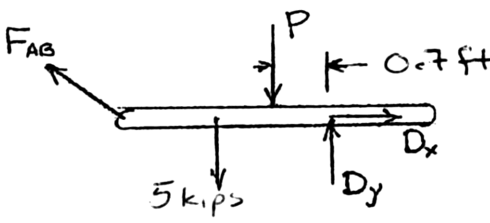
$$A_{AC} = \frac{(\text{F.S.})F_{AC}}{\sigma_U} = \frac{(3.97)(20 \times 10^3)}{300 \times 10^6} = 264.67 \times 10^{-6} \text{ m}^2 \quad A_{AC} = 265 \text{ mm}^2 \blacktriangleleft$$



**PROBLEM 1.42**

Link  $AB$  is to be made of a steel for which the ultimate normal stress is 65 ksi. Determine the cross-sectional area of  $AB$  for which the factor of safety will be 3.20. Assume that the link will be adequately reinforced around the pins at  $A$  and  $B$ .

**SOLUTION**



$$P = (4.2)(0.6) = 2.52 \text{ kips}$$

$$+\circlearrowleft \Sigma M_D = 0 : \quad -(2.8)(F_{AB} \sin 35^\circ) + (0.7)(2.52) + (1.4)(5) = 0$$

$$F_{AB} = 5.4570 \text{ kips}$$

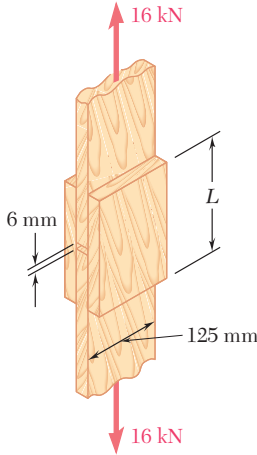
$$\sigma_{AB} = \frac{F_{AB}}{A_{AB}} = \frac{\sigma_{ult}}{F.S.}$$

$$A_{AB} = \frac{(F.S.)F_{AB}}{\sigma_{ult}} = \frac{(3.20)(5.4570 \text{ kips})}{65 \text{ ksi}} = 0.26854 \text{ in}^2$$

$A_{AB} = 0.268 \text{ in}^2 \blacktriangleleft$



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The diagram shows two vertical wooden members of width 125 mm. They are joined by two horizontal plywood splice plates, one on each side. The splice plates are fully glued to the contact surfaces. There is a 6 mm gap between the ends of the two wooden members. The length of the splice plates is denoted as L. A 16 kN force is applied upwards at the top and downwards at the bottom of the members.

**PROBLEM 1.43**

Two wooden members are joined by plywood splice plates that are fully glued on the contact surfaces. Knowing that the clearance between the ends of the members is 6 mm and that the ultimate shearing stress in the glued joint is 2.5 MPa, determine the length  $L$  for which the factor of safety is 2.75 for the loading shown.

**SOLUTION**

$$\tau_{\text{all}} = \frac{2.5 \text{ MPa}}{2.75} = 0.90909 \text{ MPa}$$

On one face of the upper contact surface,

$$A = \frac{L - 0.006 \text{ m}}{2} (0.125 \text{ m})$$

Since there are 2 contact surfaces,

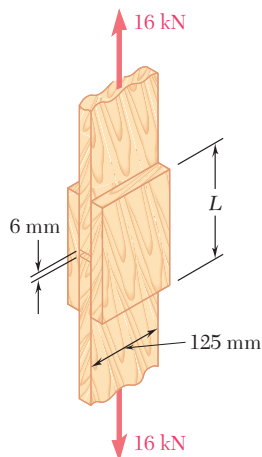
$$\tau_{\text{all}} = \frac{P}{2A}$$

$$0.90909 \times 10^6 = \frac{16 \times 10^3}{(L - 0.006)(0.125)}$$

$$L = 0.14680 \text{ m}$$

146.8 mm ◀

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Full file at <https://TestbankDirect.eu/>**PROBLEM 1.44**

For the joint and loading of Prob. 1.43, determine the factor of safety when  $L = 180$  mm.

**PROBLEM 1.43** Two wooden members are joined by plywood splice plates that are fully glued on the contact surfaces. Knowing that the clearance between the ends of the members is 6 mm and that the ultimate shearing stress in the glued joint is 2.5 MPa, determine the length  $L$  for which the factor of safety is 2.75 for the loading shown.

**SOLUTION**

Area of one face of upper contact surface:

$$A = \frac{0.180 \text{ m} - 0.006 \text{ m}}{2} (0.125 \text{ m})$$

$$A = 10.8750 \times 10^{-3} \text{ m}^2$$

Since there are two surfaces,

$$\tau_{\text{all}} = \frac{P}{2A} = \frac{16 \times 10^3 \text{ N}}{2(10.8750 \times 10^{-3} \text{ m}^2)}$$

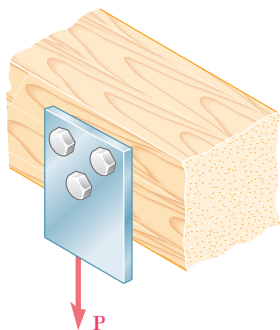
$$\tau_{\text{all}} = 0.73563 \text{ MPa}$$

$$\text{F.S.} = \frac{\tau_u}{\tau_{\text{all}}} = \frac{2.5 \text{ MPa}}{0.73563 \text{ MPa}} = 3.40$$

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Three  $\frac{3}{4}$ -in.-diameter steel bolts are to be used to attach the steel plate shown to a wooden beam. Knowing that the plate will support a load  $P = 24$  kips and that the ultimate shearing stress for the steel used is 52 ksi, determine the factor of safety for this design.

**SOLUTION**

For each bolt, 
$$A = \frac{\pi}{4}d^2 = \frac{\pi}{4}\left(\frac{3}{4}\right)^2 = 0.44179 \text{ in}^2$$

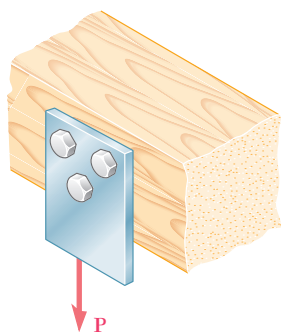
$$\begin{aligned} P_U &= A\tau_U = (0.44179)(52) \\ &= 22.973 \text{ kips} \end{aligned}$$

For the three bolts, 
$$P_U = (3)(22.973) = 68.919 \text{ kips}$$

Factor of safety:

$$F.S. = \frac{P_U}{P} = \frac{68.919}{24} \qquad F.S. = 2.87 \blacktriangleleft$$

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Full file at <https://TestbankDirect.eu/>**PROBLEM 1.46**

Three steel bolts are to be used to attach the steel plate shown to a wooden beam. Knowing that the plate will support a load  $P = 28$  kips, that the ultimate shearing stress for the steel used is 52 ksi, and that a factor of safety of 3.25 is desired, determine the required diameter of the bolts.

**SOLUTION**

For each bolt, 
$$P = \frac{28}{3} = 9.33 \text{ kips}$$

Required: 
$$P_U = (F.S.)P = (3.25)(9.33) = 30.32 \text{ kips}$$

$$\tau_U = \frac{P_U}{A} = \frac{P_U}{\frac{\pi}{4}d^2} = \frac{4P_U}{\pi d^2}$$

$$d = \sqrt{\frac{4P_U}{\pi\tau_U}} = \sqrt{\frac{(4)(30.32)}{\pi(52)}} = 0.79789 \text{ in.} \quad d = 0.798 \text{ in.} \blacktriangleleft$$

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**PROBLEM 1.47**

A load  $P$  is supported as shown by a steel pin that has been inserted in a short wooden member hanging from the ceiling. The ultimate strength of the wood used is 60 MPa in tension and 7.5 MPa in shear, while the ultimate strength of the steel is 145 MPa in shear. Knowing that  $b = 40$  mm,  $c = 55$  mm, and  $d = 12$  mm, determine the load  $P$  if an overall factor of safety of 3.2 is desired.

**SOLUTION**

Based on double shear in pin,

$$\begin{aligned}
 P_U &= 2A\tau_U = 2\frac{\pi}{4}d^2\tau_U \\
 &= \frac{\pi}{4}(2)(0.012)^2(145 \times 10^6) = 32.80 \times 10^3 \text{ N}
 \end{aligned}$$

Based on tension in wood,

$$\begin{aligned}
 P_U &= A\sigma_U = w(b-d)\sigma_U \\
 &= (0.040)(0.040 - 0.012)(60 \times 10^6) \\
 &= 67.2 \times 10^3 \text{ N}
 \end{aligned}$$

Based on double shear in the wood,

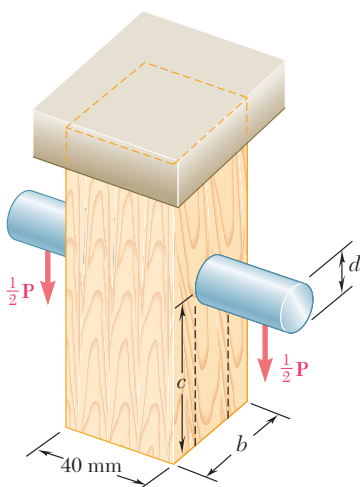
$$\begin{aligned}
 P_U &= 2A\tau_U = 2wc\tau_U = (2)(0.040)(0.055)(7.5 \times 10^6) \\
 &= 33.0 \times 10^3 \text{ N}
 \end{aligned}$$

Use smallest

$$P_U = 32.8 \times 10^3 \text{ N}$$

Allowable:

$$P = \frac{P_U}{F.S.} = \frac{32.8 \times 10^3}{3.2} = 10.25 \times 10^3 \text{ N} \quad \blacktriangleleft$$



**PROBLEM 1.48**

For the support of Prob. 1.47, knowing that the diameter of the pin is  $d = 16 \text{ mm}$  and that the magnitude of the load is  $P = 20 \text{ kN}$ , determine (a) the factor of safety for the pin, (b) the required values of  $b$  and  $c$  if the factor of safety for the wooden members is the same as that found in part a for the pin.

**PROBLEM 1.47** A load  $P$  is supported as shown by a steel pin that has been inserted in a short wooden member hanging from the ceiling. The ultimate strength of the wood used is  $60 \text{ MPa}$  in tension and  $7.5 \text{ MPa}$  in shear, while the ultimate strength of the steel is  $145 \text{ MPa}$  in shear. Knowing that  $b = 40 \text{ mm}$ ,  $c = 55 \text{ mm}$ , and  $d = 12 \text{ mm}$ , determine the load  $P$  if an overall factor of safety of  $3.2$  is desired.

**SOLUTION**

$$P = 20 \text{ kN} = 20 \times 10^3 \text{ N}$$

(a) Pin:

$$A = \frac{\pi}{4} d^2 = \frac{\pi}{4} (0.016)^2 = 2.0106 \times 10^{-6} \text{ m}^2$$

Double shear:

$$\tau = \frac{P}{2A} \quad \tau_U = \frac{P_U}{2A}$$

$$P_U = 2A\tau_U = (2)(2.0106 \times 10^{-6})(145 \times 10^6) = 58.336 \times 10^3 \text{ N}$$

$$F.S. = \frac{P_U}{P} = \frac{58.336 \times 10^3}{20 \times 10^3} \quad F.S. = 2.92 \blacktriangleleft$$

(b) Tension in wood:

$$P_U = 58.336 \times 10^3 \text{ N} \quad \text{for same F.S.}$$

$$\sigma_U = \frac{P_U}{A} = \frac{P_U}{w(b-d)} \quad \text{where } w = 40 \text{ mm} = 0.040 \text{ m}$$

$$b = d + \frac{P_U}{w\sigma_U} = 0.016 + \frac{58.336 \times 10^3}{(0.040)(60 \times 10^6)} = 40.3 \times 10^{-3} \text{ m} \quad b = 40.3 \text{ mm} \blacktriangleleft$$

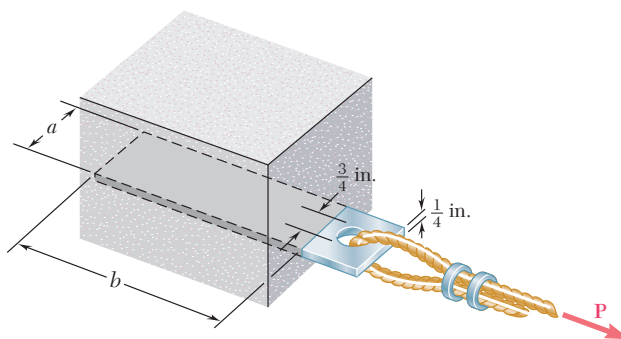
Shear in wood:

$$P_U = 58.336 \times 10^3 \text{ N} \quad \text{for same F.S.}$$

Double shear: each area is  $A = wc$

$$\tau_U = \frac{P_U}{2A} = \frac{P_U}{2wc}$$

$$c = \frac{P_U}{2w\tau_U} = \frac{58.336 \times 10^3}{(2)(0.040)(7.5 \times 10^6)} = 97.2 \times 10^{-3} \text{ m} \quad c = 97.2 \text{ mm} \blacktriangleleft$$

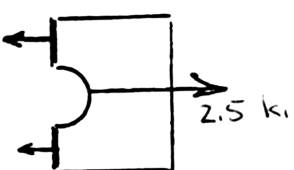


### PROBLEM 1.49

A steel plate  $\frac{1}{4}$  in. thick is embedded in a concrete wall to anchor a high-strength cable as shown. The diameter of the hole in the plate is  $\frac{3}{4}$  in., the ultimate strength of the steel used is 36 ksi, and the ultimate bonding stress between plate and concrete is 300 psi. Knowing that a factor of safety of 3.60 is desired when  $P = 2.5$  kips, determine (a) the required width  $a$  of the plate, (b) the minimum depth  $b$  to which a plate of that width should be embedded in the concrete slab. (Neglect the normal stresses between the concrete and the end of the plate.)

### SOLUTION

Based on tension in plate,



$$A = (a - d)t$$

$$P_U = \sigma_U A$$

$$F.S. = \frac{P_U}{P} = \frac{\sigma_U(a - d)t}{P}$$

Solving for  $a$ ,

$$a = d + \frac{(F.S.)P}{\sigma_U t} = \frac{3}{4} + \frac{(3.60)(2.5)}{(36)(\frac{1}{4})}$$

(a)  $a = 1.750$  in. ◀

Based on shear between plate and concrete slab,

$$A = \text{perimeter} \times \text{depth} = 2(a + t)b \quad \tau_U = 0.300 \text{ ksi}$$

$$P_U = \tau_U A = 2\tau_U(a + t)b \quad F.S. = \frac{P_U}{P}$$

Solving for  $b$ ,

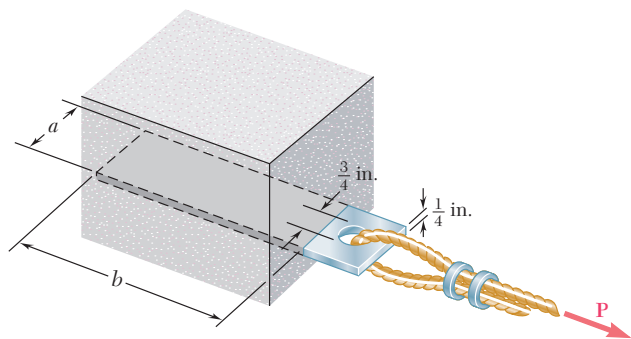
$$b = \frac{(F.S.)P}{2(a + t)\tau_U} = \frac{(3.6)(2.5)}{(2)(1.75 + \frac{1}{4})(0.300)}$$

(b)  $b = 7.50$  in. ◀

**PROBLEM 1.50**

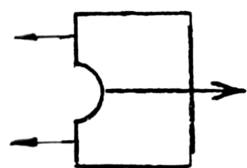
Determine the factor of safety for the cable anchor in Prob. 1.49 when  $P = 2.5$  kips, knowing that  $a = 2$  in. and  $b = 6$  in.

**PROBLEM 1.49** A steel plate  $\frac{1}{4}$  in. thick is embedded in a concrete wall to anchor a high-strength cable as shown. The diameter of the hole in the plate is  $\frac{3}{4}$  in., the ultimate strength of the steel used is 36 ksi, and the ultimate bonding stress between plate and concrete is 300 psi. Knowing that a factor of safety of 3.60 is desired when  $P = 2.5$  kips, determine (a) the required width  $a$  of the plate, (b) the minimum depth  $b$  to which a plate of that width should be embedded in the concrete slab. (Neglect the normal stresses between the concrete and the end of the plate.)



**SOLUTION**

Based on tension in plate,



$$\begin{aligned}
 A &= (a - d)t \\
 &= \left(2 - \frac{3}{4}\right)\left(\frac{1}{4}\right) = 0.31250 \text{ in}^2 \\
 P_U &= \sigma_U A \\
 &= (36)(0.31250) = 11.2500 \text{ kips} \\
 F.S. &= \frac{P_U}{P} = \frac{11.2500}{2.5} = 4.50
 \end{aligned}$$

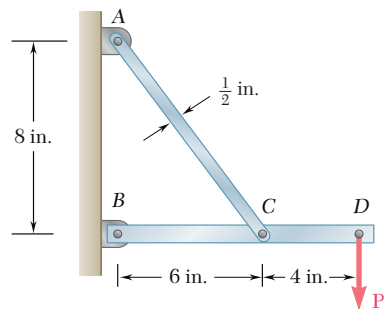
Based on shear between plate and concrete slab,

$$\begin{aligned}
 A &= \text{perimeter} \times \text{depth} = 2(a + t)b = 2\left(2 + \frac{1}{4}\right)(6.0) \\
 A &= 27.0 \text{ in}^2 \quad \tau_U = 0.300 \text{ ksi} \\
 P_U &= \tau_U A = (0.300)(27.0) = 8.10 \text{ kips} \\
 F.S. &= \frac{P_U}{P} = \frac{8.10}{2.5} = 3.240
 \end{aligned}$$

Actual factor of safety is the smaller value.

$F.S. = 3.24 \blacktriangleleft$



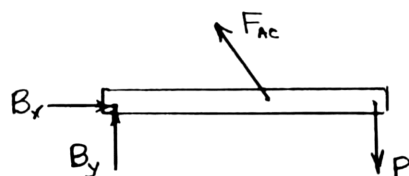


### PROBLEM 1.51

Link  $AC$  is made of a steel with a 65-ksi ultimate normal stress and has a  $\frac{1}{4} \times \frac{1}{2}$ -in. uniform rectangular cross section. It is connected to a support at  $A$  and to member  $BCD$  at  $C$  by  $\frac{3}{4}$ -in.-diameter pins, while member  $BCD$  is connected to its support at  $B$  by a  $\frac{5}{16}$ -in.-diameter pin. All of the pins are made of a steel with a 25-ksi ultimate shearing stress and are in single shear. Knowing that a factor of safety of 3.25 is desired, determine the largest load  $P$  that can be applied at  $D$ . Note that link  $AC$  is not reinforced around the pin holes.

### SOLUTION

Use free body  $BCD$ .



$$+\curvearrowright M_B = 0: \quad (6) \left( \frac{8}{10} F_{AC} \right) - 10P = 0$$

$$P = 0.48 F_{AC} \quad (1)$$

$$+\rightarrow \Sigma F_x = 0: \quad B_x - \frac{6}{10} F_{AC} = 0$$

$$B_x = \frac{6}{10} F_{AC} = 1.25P \rightarrow$$

$$+\curvearrowright M_C = 0: \quad -6B_y - 4P = 0$$

$$B_y = -\frac{2}{3}P \quad \text{i.e.} \quad B_y = \frac{2}{3}P \downarrow$$

$$B = \sqrt{B_x^2 + B_y^2} = \sqrt{1.25^2 + \left(\frac{2}{3}\right)^2} P = 1.41667P \quad P = 0.70588B \quad (2)$$

Shear in pins at  $A$  and  $C$ .

$$F_{AC} = \tau A_{\text{pin}} = \frac{\tau_U}{F.S.} \frac{\pi}{4} d^2 = \left( \frac{25}{3.25} \right) \left( \frac{\pi}{4} \right) \left( \frac{3}{8} \right)^2 = 0.84959 \text{ kips}$$

Tension on net section of  $A$  and  $C$ .

$$F_{AC} = \sigma A_{\text{net}} = \frac{\sigma_U}{F.S.} A_{\text{net}} = \left( \frac{65}{3.25} \right) \left( \frac{1}{4} \right) \left( \frac{1}{2} - \frac{3}{8} \right) = 0.625 \text{ kips}$$

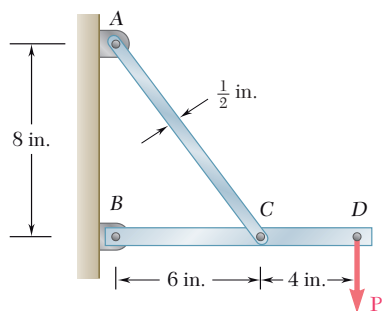
Smaller value of  $F_{AC}$  is 0.625 kips.

From (1),  $P = (0.48)(0.625) = 0.300$  kips

Shear in pin at  $B$ .  $B = \tau A_{\text{pin}} = \frac{\tau_U}{F.S.} \frac{\pi}{4} d^2 = \left( \frac{25}{3.25} \right) \left( \frac{\pi}{4} \right) \left( \frac{5}{16} \right)^2 = 0.58999$  kips

From (2),  $P = (0.70588)(0.58999) = 0.416$  kips

Allowable value of  $P$  is the smaller value.  $P = 0.300$  kips or  $P = 300$  lb ◀



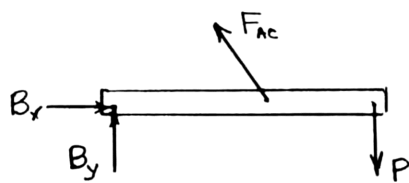
### PROBLEM 1.52

Solve Prob. 1.51, assuming that the structure has been redesigned to use  $\frac{5}{16}$ -in.-diameter pins at  $A$  and  $C$  as well as at  $B$  and that no other changes have been made.

**PROBLEM 1.51** Link  $AC$  is made of a steel with a 65-ksi ultimate normal stress and has a  $\frac{1}{4} \times \frac{1}{2}$ -in. uniform rectangular cross section. It is connected to a support at  $A$  and to member  $BCD$  at  $C$  by  $\frac{3}{4}$ -in.-diameter pins, while member  $BCD$  is connected to its support at  $B$  by a  $\frac{5}{16}$ -in.-diameter pin. All of the pins are made of a steel with a 25-ksi ultimate shearing stress and are in single shear. Knowing that a factor of safety of 3.25 is desired, determine the largest load  $P$  that can be applied at  $D$ . Note that link  $AC$  is not reinforced around the pin holes.

### SOLUTION

Use free body  $BCD$ .



$$+\curvearrowright M_B = 0 : (6) \left( \frac{8}{10} F_{AC} \right) - 10P = 0$$

$$P = 0.48 F_{AC} \quad (1)$$

$$+\uparrow \Sigma F_y = 0 : B_x - \frac{6}{10} F_{AC} = 0$$

$$B_x = \frac{6}{10} F_{AC} = 1.25P \rightarrow$$

$$+\curvearrowright M_C = 0 : -6B_y - 4P = 0$$

$$B_y = -\frac{2}{3}P \quad \text{i.e.} \quad B_y = \frac{2}{3}P \downarrow$$

$$B = \sqrt{B_x^2 + B_y^2} = \sqrt{1.25^2 + \left(\frac{2}{3}\right)^2} P = 1.41667P \quad P = 0.70583B \quad (2)$$

Shear in pins at  $A$  and  $C$ .

$$F_{AC} = \tau A_{\text{pin}} = \frac{\tau_U}{F.S.} \frac{\pi}{4} d^2 = \left( \frac{25}{3.25} \right) \left( \frac{\pi}{4} \right) \left( \frac{5}{16} \right)^2 = 0.58999 \text{ kips}$$

Tension on net section of  $A$  and  $C$ .

$$F_{AC} = \sigma A_{\text{net}} = \frac{\sigma_U}{F.S.} A_{\text{net}} = \left( \frac{65}{3.25} \right) \left( \frac{1}{4} \right) \left( \frac{1}{2} - \frac{5}{16} \right) = 0.9375 \text{ kips}$$

Smaller value of  $F_{AC}$  is 0.58999 kips.

From (1),  $P = (0.48)(0.58999) = 0.283 \text{ kips}$

Shear in pin at  $B$ .  $B = \tau A_{\text{pin}} = \frac{\tau_U}{F.S.} \frac{\pi}{4} d^2 = \left( \frac{25}{3.25} \right) \left( \frac{\pi}{4} \right) \left( \frac{5}{16} \right)^2 = 0.58999 \text{ kips}$

From (2),  $P = (0.70588)(0.58999) = 0.416 \text{ kips}$

Allowable value of  $P$  is the smaller value.  $P = 0.283 \text{ kips}$  or  $P = 283 \text{ lb} \blacktriangleleft$

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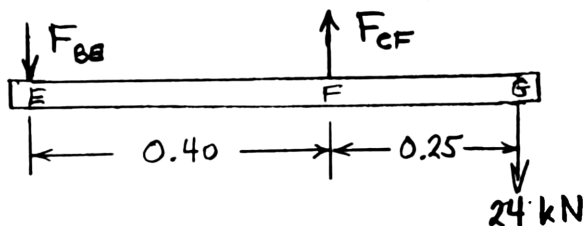
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**PROBLEM 1.53**

Each of the two vertical links  $CF$  connecting the two horizontal members  $AD$  and  $EG$  has a  $10 \times 40$ -mm uniform rectangular cross section and is made of a steel with an ultimate strength in tension of 400 MPa, while each of the pins at  $C$  and  $F$  has a 20-mm diameter and are made of a steel with an ultimate strength in shear of 150 MPa. Determine the overall factor of safety for the links  $CF$  and the pins connecting them to the horizontal members.

**SOLUTION**

Use member EFG as free body.



$$\begin{aligned} +\curvearrowright \Sigma M_E = 0 : \quad & 0.40F_{CF} - (0.65)(24 \times 10^3) = 0 \\ & F_{CF} = 39 \times 10^3 \text{ N} \end{aligned}$$

Based on tension in links  $CF$ ,

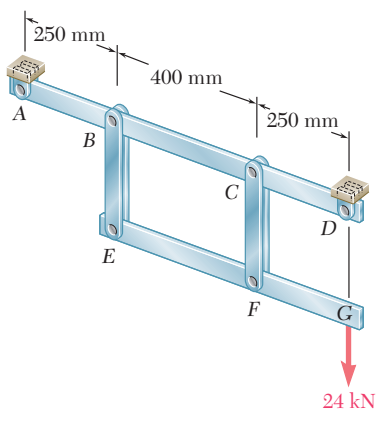
$$\begin{aligned} A &= (b - d)t = (0.040 - 0.02)(0.010) = 200 \times 10^{-6} \text{ m}^2 \quad (\text{one link}) \\ F_U &= 2\sigma_U A = (2)(400 \times 10^6)(200 \times 10^{-6}) = 160.0 \times 10^3 \text{ N} \end{aligned}$$

Based on double shear in pins,

$$\begin{aligned} A &= \frac{\pi}{4} d^2 = \frac{\pi}{4} (0.020)^2 = 314.16 \times 10^{-6} \text{ m}^2 \\ F_U &= 2\tau_U A = (2)(150 \times 10^6)(314.16 \times 10^{-6}) = 94.248 \times 10^3 \text{ N} \end{aligned}$$

Actual  $F_U$  is smaller value, i.e.  $F_U = 94.248 \times 10^3 \text{ N}$

Factor of safety: 
$$F.S. = \frac{F_U}{F_{CF}} = \frac{94.248 \times 10^3}{39 \times 10^3} \qquad F.S. = 2.42 \blacktriangleleft$$



**PROBLEM 1.54**

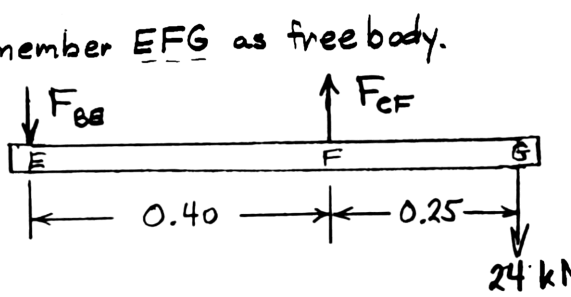
Solve Prob. 1.53, assuming that the pins at  $C$  and  $F$  have been replaced by pins with a 30-mm diameter.

**PROBLEM 1.53** Each of the two vertical links  $CF$  connecting the two horizontal members  $AD$  and  $EG$  has a  $10 \times 40$ -mm uniform rectangular cross section and is made of a steel with an ultimate strength in tension of 400 MPa, while each of the pins at  $C$  and  $F$  has a 20-mm diameter and are made of a steel with an ultimate strength in shear of 150 MPa. Determine the overall factor of safety for the links  $CF$  and the pins connecting them to the horizontal members.

**SOLUTION**

Use member  $EFG$  as free body.

Use member EFG as free body.



$$+\circlearrowleft \sum M_E = 0: 0.40F_{CF} - (0.65)(24 \times 10^3) = 0$$

$$F_{CF} = 39 \times 10^3 \text{ N}$$

Based on tension in links  $CF$ ,

$$A = (b - d)t = (0.040 - 0.030)(0.010) = 100 \times 10^{-6} \text{ m}^2 \quad (\text{one link})$$

$$F_U = 2\sigma_U A = (2)(400 \times 10^6)(100 \times 10^{-6}) = 80.0 \times 10^3 \text{ N}$$

Based on double shear in pins,

$$A = \frac{\pi}{4}d^2 = \frac{\pi}{4}(0.030)^2 = 706.86 \times 10^{-6} \text{ m}^2$$

$$F_U = 2\tau_U A = (2)(150 \times 10^6)(706.86 \times 10^{-6}) = 212.06 \times 10^3 \text{ N}$$

Actual  $F_U$  is smaller value, i.e.  $F_U = 80.0 \times 10^3 \text{ N}$

Factor of safety: 
$$F.S. = \frac{F_U}{F_{CF}} = \frac{80.0 \times 10^3}{39 \times 10^3} \quad F.S. = 2.05 \blacktriangleleft$$

### PROBLEM 1.55

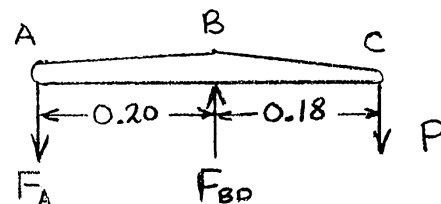
In the structure shown, an 8-mm-diameter pin is used at *A*, and 12-mm-diameter pins are used at *B* and *D*. Knowing that the ultimate shearing stress is 100 MPa at all connections and that the ultimate normal stress is 250 MPa in each of the two links joining *B* and *D*, determine the allowable load *P* if an overall factor of safety of 3.0 is desired.

### SOLUTION

Statics: Use *ABC* as free body.

$$+\curvearrowright \Sigma M_B = 0 : 0.20F_A - 0.18P = 0 \quad P = \frac{10}{9}F_A$$

$$+\curvearrowright \Sigma M_A = 0 : 0.20F_{BD} - 0.38P = 0 \quad P = \frac{10}{19}F_{BD}$$



Based on double shear in pin *A*,  $A = \frac{\pi}{4}d^2 = \frac{\pi}{4}(0.008)^2 = 50.266 \times 10^{-6} \text{ m}^2$

$$F_A = \frac{2\tau_U A}{F.S.} = \frac{(2)(100 \times 10^6)(50.266 \times 10^{-6})}{3.0} = 3.351 \times 10^3 \text{ N}$$

$$P = \frac{10}{9}F_A = 3.72 \times 10^3 \text{ N}$$

Based on double shear in pins at *B* and *D*,  $A = \frac{\pi}{4}d^2 = \frac{\pi}{4}(0.012)^2 = 113.10 \times 10^{-6} \text{ m}^2$

$$F_{BD} = \frac{2\tau_U A}{F.S.} = \frac{(2)(100 \times 10^6)(113.10 \times 10^{-6})}{3.0} = 7.54 \times 10^3 \text{ N}$$

$$P = \frac{10}{19}F_{BD} = 3.97 \times 10^3 \text{ N}$$

Based on compression in links *BD*, for one link,  $A = (0.020)(0.008) = 160 \times 10^{-6} \text{ m}^2$

$$F_{BD} = \frac{2\sigma_U A}{F.S.} = \frac{(2)(250 \times 10^6)(160 \times 10^{-6})}{3.0} = 26.7 \times 10^3 \text{ N}$$

$$P = \frac{10}{19}F_{BD} = 14.04 \times 10^3 \text{ N}$$

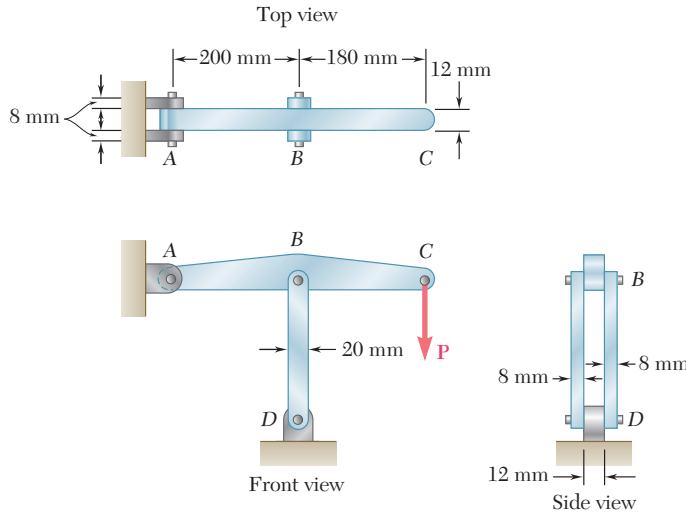
Allowable value of *P* is smallest,  $\therefore P = 3.72 \times 10^3 \text{ N}$

$P = 3.72 \text{ kN} \blacktriangleleft$

**PROBLEM 1.56**

In an alternative design for the structure of Prob. 1.55, a pin of 10-mm-diameter is to be used at *A*. Assuming that all other specifications remain unchanged, determine the allowable load **P** if an overall factor of safety of 3.0 is desired.

**PROBLEM 1.55** In the structure shown, an 8-mm-diameter pin is used at *A*, and 12-mm-diameter pins are used at *B* and *D*. Knowing that the ultimate shearing stress is 100 MPa at all connections and that the ultimate normal stress is 250 MPa in each of the two links joining *B* and *D*, determine the allowable load **P** if an overall factor of safety of 3.0 is desired.

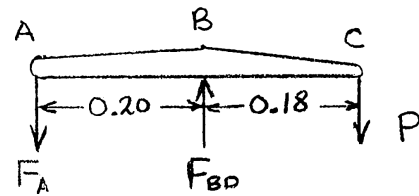


**SOLUTION**

Statics: Use *ABC* as free body.

$$+\circlearrowleft \Sigma M_B = 0: \quad 0.20F_A - 0.18P = 0 \quad P = \frac{10}{9}F_A$$

$$+\circlearrowleft \Sigma M_A = 0: \quad 0.20F_{BD} - 0.38P = 0 \quad P = \frac{10}{19}F_{BD}$$



Based on double shear in pin *A*,  $A = \frac{\pi}{4}d^2 = \frac{\pi}{4}(0.010)^2 = 78.54 \times 10^{-6} \text{ m}^2$

$$F_A = \frac{2\tau_U A}{F.S.} = \frac{(2)(100 \times 10^6)(78.54 \times 10^{-6})}{3.0} = 5.236 \times 10^3 \text{ N}$$

$$P = \frac{10}{9}F_A = 5.82 \times 10^3 \text{ N}$$

Based on double shear in pins at *B* and *D*,  $A = \frac{\pi}{4}d^2 = \frac{\pi}{4}(0.012)^2 = 113.10 \times 10^{-6} \text{ m}^2$

$$F_{BD} = \frac{2\tau_U A}{F.S.} = \frac{(2)(100 \times 10^6)(113.10 \times 10^{-6})}{3.0} = 7.54 \times 10^3 \text{ N}$$

$$P = \frac{10}{19}F_{BD} = 3.97 \times 10^3 \text{ N}$$

Based on compression in links *BD*, for one link,  $A = (0.020)(0.008) = 160 \times 10^{-6} \text{ m}^2$

$$F_{BD} = \frac{2\sigma_U A}{F.S.} = \frac{(2)(250 \times 10^6)(160 \times 10^{-6})}{3.0} = 26.7 \times 10^3 \text{ N}$$

$$P = \frac{10}{19}F_{BD} = 14.04 \times 10^3 \text{ N}$$

Allowable value of *P* is smallest,  $\therefore P = 3.97 \times 10^3 \text{ N}$

$P = 3.97 \text{ kN} \blacktriangleleft$

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### PROBLEM 1.57

A 40-kg platform is attached to the end  $B$  of a 50-kg wooden beam  $AB$ , which is supported as shown by a pin at  $A$  and by a slender steel rod  $BC$  with a 12-kN ultimate load. (a) Using the Load and Resistance Factor Design method with a resistance factor  $\phi = 0.90$  and load factors  $\gamma_D = 1.25$  and  $\gamma_L = 1.6$ , determine the largest load that can be safely placed on the platform. (b) What is the corresponding conventional factor of safety for rod  $BC$ ?

### SOLUTION

$$+\circlearrowleft \Sigma M_A = 0: (2.4)\frac{3}{5}P - 2.4W_1 - 1.2W_2$$

$$\therefore P = \frac{5}{3}W_1 + \frac{5}{6}W_2$$

For dead loading,  $W_1 = (40)(9.81) = 392.4 \text{ N}$ ,  $W_2 = (50)(9.81) = 490.5 \text{ N}$

$$P_D = \left(\frac{5}{3}\right)(392.4) + \left(\frac{5}{6}\right)(490.5) = 1.0628 \times 10^3 \text{ N}$$

For live loading,  $W_1 = mg$ ,  $W_2 = 0$ ,  $P_L = \frac{5}{3}mg$

From which  $m = \frac{3}{5} \frac{P_L}{g}$

Design criterion:  $\gamma_D P_D + \gamma_L P_L = \phi P_U$

$$P_L = \frac{\phi P_U - \gamma_D P_D}{\gamma_L} = \frac{(0.90)(12 \times 10^3) - (1.25)(1.0628 \times 10^3)}{1.6}$$

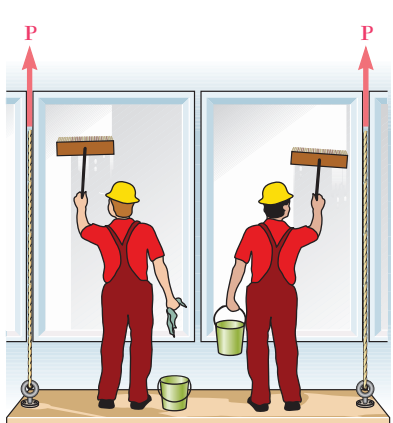
$$= 5.920 \times 10^3 \text{ N}$$

(a) Allowable load.  $m = \frac{3}{5} \frac{5.92 \times 10^3}{9.81}$   $m = 362 \text{ kg} \blacktriangleleft$

Conventional factor of safety:

$$P = P_D + P_L = 1.0628 \times 10^3 + 5.920 \times 10^3 = 6.983 \times 10^3 \text{ N}$$

(b)  $F.S. = \frac{P_U}{P} = \frac{12 \times 10^3}{6.983 \times 10^3}$   $F.S. = 1.718 \blacktriangleleft$

Full file at <https://TestbankDirect.eu/>


**PROBLEM 1.58**

The Load and Resistance Factor Design method is to be used to select the two cables that will raise and lower a platform supporting two window washers. The platform weighs 160 lb and each of the window washers is assumed to weigh 195 lb with equipment. Since these workers are free to move on the platform, 75% of their total weight and the weight of their equipment will be used as the design live load of each cable. (a) Assuming a resistance factor  $\phi = 0.85$  and load factors  $\gamma_D = 1.2$  and  $\gamma_L = 1.5$ , determine the required minimum ultimate load of one cable. (b) What is the corresponding conventional factor of safety for the selected cables?

**SOLUTION**

$$\gamma_D P_D + \gamma_L P_L = \phi P_U$$

$$(a) \quad P_U = \frac{\gamma_D P_D + \gamma_L P_L}{\phi}$$

$$= \frac{(1.2) \left( \frac{1}{2} \times 160 \right) + (1.5) \left( \frac{3}{4} \times 2 \times 195 \right)}{0.85} \quad P_U = 629 \text{ lb} \blacktriangleleft$$

Conventional factor of safety:

$$P = P_D + P_L = \frac{1}{2} \times 160 + 0.75 \times 2 \times 195 = 372.5 \text{ lb}$$

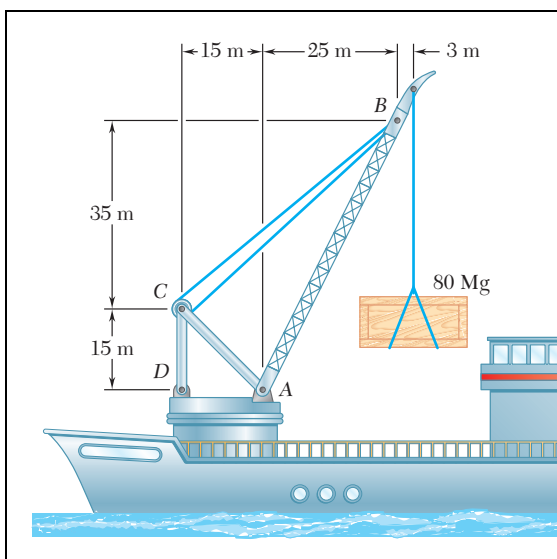
$$(b) \quad F.S. = \frac{P_U}{P} = \frac{629}{372.5} \quad F.S. = 1.689 \blacktriangleleft$$

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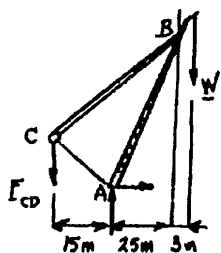
### PROBLEM 1.59

In the marine crane shown, link  $CD$  is known to have a uniform cross section of  $50 \times 150$  mm. For the loading shown, determine the normal stress in the central portion of that link.

### SOLUTION

Weight of loading:  $W = (80 \text{ Mg})(9.81 \text{ m/s}^2) = 784.8 \text{ kN}$

Free Body: Portion  $ABC$ .



$$\begin{aligned} +\curvearrowright \sum M_A = 0: & F_{CD}(15 \text{ m}) - W(28 \text{ m}) = 0 \\ F_{CD} = \frac{28}{15}W = \frac{28}{15}(784.8 \text{ kN}) \\ F_{CD} = & +1465 \text{ kN} \end{aligned}$$

$$\sigma_{CD} = \frac{F_{CD}}{A} = \frac{+1465 \times 10^3 \text{ N}}{(0.050 \text{ m})(0.150 \text{ m})} = +195.3 \times 10^6 \text{ Pa} \quad \sigma_{CD} = +195.3 \text{ MPa} \blacktriangleleft$$

### PROBLEM 1.60

Two horizontal 5-kip forces are applied to pin  $B$  of the assembly shown. Knowing that a pin of 0.8-in. diameter is used at each connection, determine the maximum value of the average normal stress (a) in link  $AB$ , (b) in link  $BC$ .

### SOLUTION

Use joint  $B$  as free body.

Law of Sines:

$$\frac{F_{AB}}{\sin 45^\circ} = \frac{F_{BC}}{\sin 60^\circ} = \frac{10}{\sin 95^\circ}$$

$$F_{AB} = 7.3205 \text{ kips}$$

$$F_{BC} = 8.9658 \text{ kips}$$

Link  $AB$  is a tension member.

Minimum section at pin:  $A_{\text{net}} = (1.8 - 0.8)(0.5) = 0.5 \text{ in}^2$

(a) Stress in  $AB$ :  $\sigma_{AB} = \frac{F_{AB}}{A_{\text{net}}} = \frac{7.3205}{0.5} \quad \sigma_{AB} = 14.64 \text{ ksi} \blacktriangleleft$

Link  $BC$  is a compression member.

Cross sectional area is  $A = (1.8)(0.5) = 0.9 \text{ in}^2$

(b) Stress in  $BC$ :  $\sigma_{BC} = \frac{-F_{BC}}{A} = \frac{-8.9658}{0.9} \quad \sigma_{BC} = -9.96 \text{ ksi} \blacktriangleleft$

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**PROBLEM 1.61**

For the assembly and loading of Prob. 1.60, determine (a) the average shearing stress in the pin at C, (b) the average bearing stress at C in member BC, (c) the average bearing stress at B in member BC.

**PROBLEM 1.60** Two horizontal 5-kip forces are applied to pin B of the assembly shown. Knowing that a pin of 0.8-in. diameter is used at each connection, determine the maximum value of the average normal stress (a) in link AB, (b) in link BC.

**SOLUTION**

Use joint B as free body.

Law of Sines:

$$\frac{F_{AB}}{\sin 45^\circ} = \frac{F_{BC}}{\sin 60^\circ} = \frac{10}{\sin 95^\circ} \quad F_{BC} = 8.9658 \text{ kips}$$

(a) Shearing stress in pin at C.  $\tau = \frac{F_{BC}}{2A_p}$

$$A_p = \frac{\pi}{4} d^2 = \frac{\pi}{4} (0.8)^2 = 0.5026 \text{ in}^2$$

$$\tau = \frac{8.9658}{(2)(0.5026)} = 8.92 \quad \tau = 8.92 \text{ ksi} \blacktriangleleft$$

Full file at <https://TestbankDirect.eu/>**PROBLEM 1.61 (Continued)**

(b) Bearing stress at C in member BC.  $\sigma_b = \frac{F_{BC}}{A}$

$$A = td = (0.5)(0.8) = 0.4 \text{ in}^2$$

$$\sigma_b = \frac{8.9658}{0.4} = 22.4$$

$$\sigma_b = 22.4 \text{ ksi} \blacktriangleleft$$

(c) Bearing stress at B in member BC.  $\sigma_b = \frac{F_{BC}}{A}$

$$A = 2td = 2(0.5)(0.8) = 0.8 \text{ in}^2$$

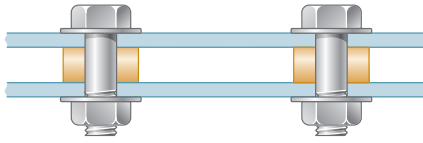
$$\sigma_b = \frac{8.9658}{0.8} = 11.21$$

$$\sigma_b = 11.21 \text{ ksi} \blacktriangleleft$$

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**PROBLEM 1.62**

Two steel plates are to be held together by means of 16-mm-diameter high-strength steel bolts fitting snugly inside cylindrical brass spacers. Knowing that the average normal stress must not exceed 200 MPa in the bolts and 130 MPa in the spacers, determine the outer diameter of the spacers that yields the most economical and safe design.

**SOLUTION**

At each bolt location the upper plate is pulled down by the tensile force  $P_b$  of the bolt. At the same time, the spacer pushes that plate upward with a compressive force  $P_s$  in order to maintain equilibrium.

$$P_b = P_s$$

$$\text{For the bolt, } \sigma_b = \frac{F_b}{A_b} = \frac{4P_b}{\pi d_b^2} \quad \text{or} \quad P_b = \frac{\pi}{4} \sigma_b d_b^2$$

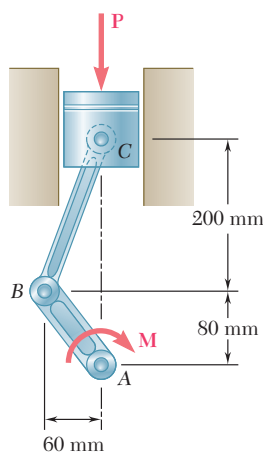
$$\text{For the spacer, } \sigma_s = \frac{P_s}{A_s} = \frac{4P_s}{\pi(d_s^2 - d_b^2)} \quad \text{or} \quad P_s = \frac{\pi}{4} \sigma_s (d_s^2 - d_b^2)$$

Equating  $P_b$  and  $P_s$ ,

$$\frac{\pi}{4} \sigma_b d_b^2 = \frac{\pi}{4} \sigma_s (d_s^2 - d_b^2)$$

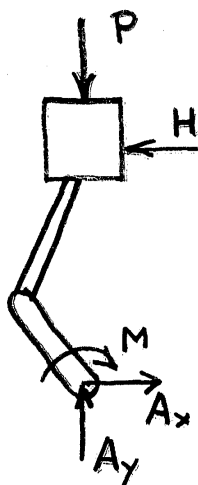
$$d_s = \sqrt{\left(1 + \frac{\sigma_b}{\sigma_s}\right)} d_b = \sqrt{\left(1 + \frac{200}{130}\right)} (16) \quad d_s = 25.2 \text{ mm} \quad \blacktriangleleft$$

**PROBLEM 1.63**



A couple  $M$  of magnitude  $1500 \text{ N} \cdot \text{m}$  is applied to the crank of an engine. For the position shown, determine (a) the force  $P$  required to hold the engine system in equilibrium, (b) the average normal stress in the connecting rod  $BC$ , which has a  $450\text{-mm}^2$  uniform cross section.

**SOLUTION**



Use piston, rod, and crank together as free body. Add wall reaction  $H$  and bearing reactions  $A_x$  and  $A_y$ .

$$+\curvearrowright \Sigma M_A = 0 : (0.280 \text{ m})H - 1500 \text{ N} \cdot \text{m} = 0$$

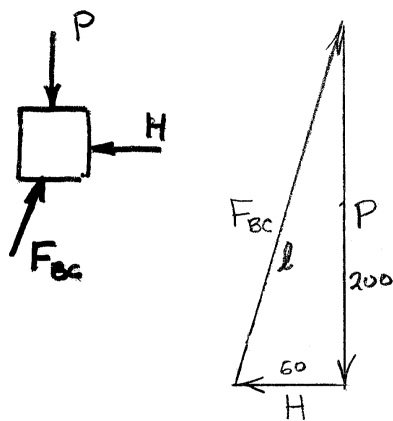
$$H = 5.3571 \times 10^3 \text{ N}$$

Use piston alone as free body. Note that rod is a two-force member; hence the direction of force  $F_{BC}$  is known. Draw the force triangle and solve for  $P$  and  $F_{BC}$  by proportions.

$$l = \sqrt{200^2 + 60^2} = 208.81 \text{ mm}$$

$$\frac{P}{H} = \frac{200}{60} \quad \therefore P = 17.86 \times 10^3 \text{ N}$$

(a)  $P = 17.86 \text{ kN} \blacktriangleleft$



$$\frac{F_{BC}}{H} = \frac{208.81}{60} \quad \therefore F_{BC} = 18.6436 \times 10^3 \text{ N}$$

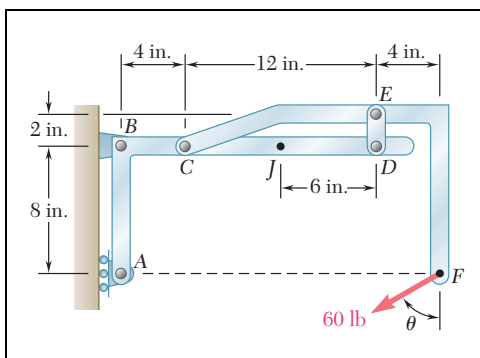
Rod  $BC$  is a compression member. Its area is

$$450 \text{ mm}^2 = 450 \times 10^{-6} \text{ m}^2$$

Stress:

$$\sigma_{BC} = \frac{-F_{BC}}{A} = \frac{-18.6436 \times 10^3}{450 \times 10^{-6}} = -41.430 \times 10^6 \text{ Pa}$$

(b)  $\sigma_{BC} = -41.4 \text{ MPa} \blacktriangleleft$

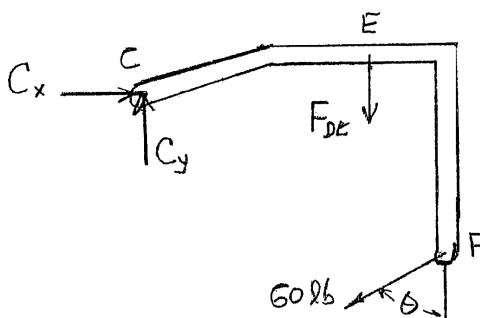


**PROBLEM 1.64**

Knowing that the link  $DE$  is  $\frac{1}{8}$  in. thick and 1 in. wide, determine the normal stress in the central portion of that link when (a)  $\theta = 0^\circ$ , (b)  $\theta = 90^\circ$ .

**SOLUTION**

Use member  $CEF$  as a free body.



$$+\circlearrowleft \sum M_C = 0 : -12 F_{DE} - (8)(60 \sin \theta) - (16)(60 \cos \theta) = 0$$

$$F_{DE} = -40 \sin \theta - 80 \cos \theta \text{ lb}$$

$$A_{DE} = (1) \left( \frac{1}{8} \right) = 0.125 \text{ in}^2$$

$$\sigma_{DE} = \frac{F_{DE}}{A_{DE}}$$

(a)  $\theta = 0^\circ$ :  $F_{DE} = -80 \text{ lb}$

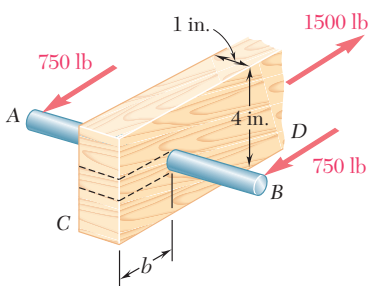
$$\sigma_{DE} = \frac{-80}{0.125}$$

$\sigma_{DE} = -640 \text{ psi} \blacktriangleleft$

(b)  $\theta = 90^\circ$ :  $F_{DE} = -40 \text{ lb}$

$$\sigma_{DE} = \frac{-40}{0.125}$$

$\sigma_{DE} = -320 \text{ psi} \blacktriangleleft$



**PROBLEM 1.65**

A  $\frac{5}{8}$ -in.-diameter steel rod  $AB$  is fitted to a round hole near end  $C$  of the wooden member  $CD$ . For the loading shown, determine (a) the maximum average normal stress in the wood, (b) the distance  $b$  for which the average shearing stress is 100 psi on the surfaces indicated by the dashed lines, (c) the average bearing stress on the wood.

**SOLUTION**

(a) Maximum normal stress in the wood.

$$A_{\text{net}} = (1) \left( 4 - \frac{5}{8} \right) = 3.375 \text{ in}^2$$

$$\sigma = \frac{P}{A_{\text{net}}} = \frac{1500}{3.375} = 444 \text{ psi} \quad \sigma = 444 \text{ psi} \blacktriangleleft$$

(b) Distance  $b$  for  $\tau = 100$  psi.  
For sheared area see dotted lines.

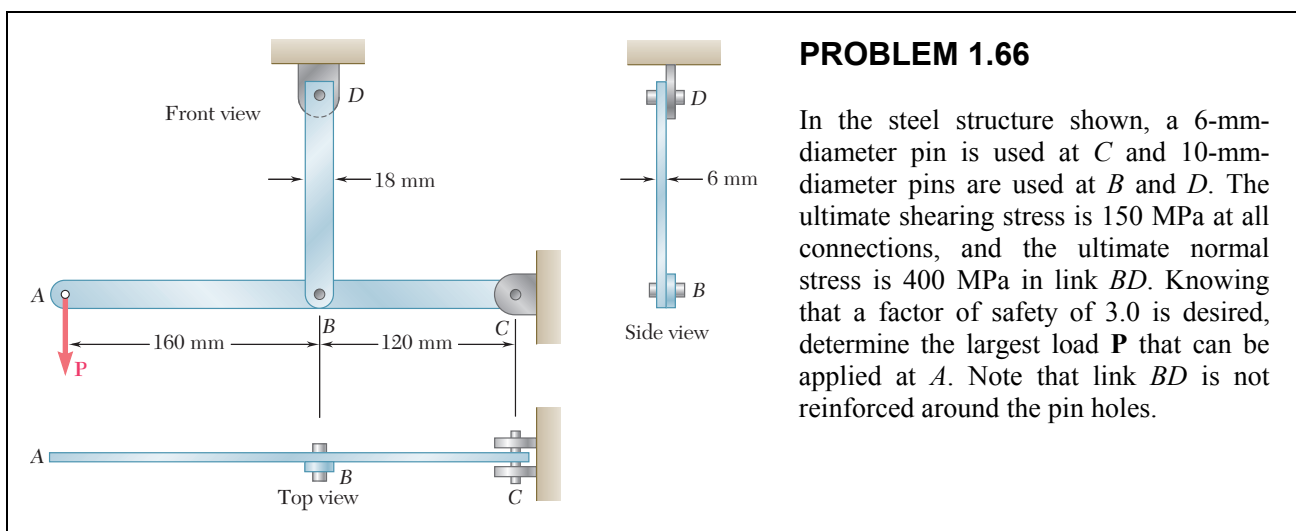
$$\tau = \frac{P}{A} = \frac{P}{2bt}$$

$$b = \frac{P}{2t\tau} = \frac{1500}{(2)(1)(100)} = 7.50 \text{ in.} \quad b = 7.50 \text{ in.} \blacktriangleleft$$

(c) Average bearing stress on the wood.

$$\sigma_b = \frac{P}{A_b} = \frac{P}{dt} = \frac{1500}{\left(\frac{5}{8}\right)(1)} = 2400 \text{ psi} \quad \sigma_b = 2400 \text{ psi} \blacktriangleleft$$



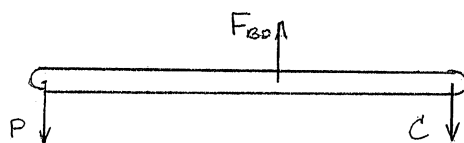


**PROBLEM 1.66**

In the steel structure shown, a 6-mm-diameter pin is used at *C* and 10-mm-diameter pins are used at *B* and *D*. The ultimate shearing stress is 150 MPa at all connections, and the ultimate normal stress is 400 MPa in link *BD*. Knowing that a factor of safety of 3.0 is desired, determine the largest load **P** that can be applied at *A*. Note that link *BD* is not reinforced around the pin holes.

**SOLUTION**

Use free body *ABC*.



$$\begin{aligned}
 +\curvearrowright \Sigma M_C = 0 : \quad & 0.280P - 0.120F_{BD} = 0 \\
 & P = \frac{3}{7}F_{BD} \qquad (1)
 \end{aligned}$$

$$\begin{aligned}
 +\curvearrowright \Sigma M_B = 0 : \quad & 0.160P - 0.120C = 0 \\
 & P = \frac{3}{4}C \qquad (2)
 \end{aligned}$$

Tension on net section of link *BD*:

$$F_{BD} = \sigma A_{\text{net}} = \frac{\sigma_U}{F.S.} A_{\text{net}} = \left( \frac{400 \times 10^6}{3} \right) (6 \times 10^{-3})(18 - 10)(10^{-3}) = 6.40 \times 10^3 \text{ N}$$

Shear in pins at *B* and *D*:

$$F_{BD} = \tau A_{\text{pin}} = \frac{\tau_U}{F.S.} \frac{\pi}{4} d^2 = \left( \frac{150 \times 10^6}{3} \right) \left( \frac{\pi}{4} \right) (10 \times 10^{-3})^2 = 3.9270 \times 10^3 \text{ N}$$

Smaller value of  $F_{BD}$  is  $3.9270 \times 10^3$  N.

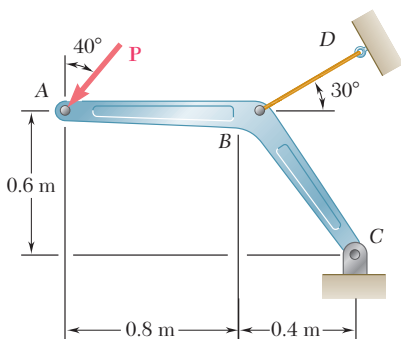
From (1), 
$$P = \left( \frac{3}{7} \right) (3.9270 \times 10^3) = 1.683 \times 10^3 \text{ N}$$

Shear in pin at *C*: 
$$C = 2\tau A_{\text{pin}} = 2 \frac{\tau_U}{F.S.} \frac{\pi}{4} d^2 = (2) \left( \frac{150 \times 10^6}{3} \right) \left( \frac{\pi}{4} \right) (6 \times 10^{-3})^2 = 2.8274 \times 10^3 \text{ N}$$

From (2), 
$$P = \left( \frac{3}{4} \right) (2.8274 \times 10^3) = 2.12 \times 10^3 \text{ N}$$

Smaller value of *P* is allowable value. 
$$P = 1.683 \times 10^3 \text{ N} \qquad P = 1.683 \text{ kN} \blacktriangleleft$$

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### PROBLEM 1.67

Member  $ABC$ , which is supported by a pin and bracket at  $C$  and a cable  $BD$ , was designed to support the 16-kN load  $P$  as shown. Knowing that the ultimate load for cable  $BD$  is 100 kN, determine the factor of safety with respect to cable failure.

### SOLUTION

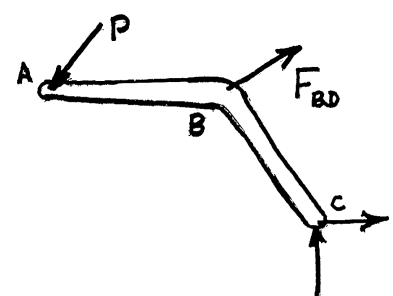
Use member  $ABC$  as a free body, and note that member  $BD$  is a two-force member.

$$\begin{aligned}
 +\curvearrowright \Sigma M_C = 0 : & (P \cos 40^\circ)(1.2) + (P \sin 40^\circ)(0.6) \\
 & - (F_{BD} \cos 30^\circ)(0.6) \\
 & - (F_{BD} \sin 30^\circ)(0.4) = 0 \\
 & 1.30493P - 0.71962F_{BD} = 0
 \end{aligned}$$
  

$$F_{BD} = 1.81335P = (1.81335)(16 \times 10^3) = 29.014 \times 10^3 \text{ N}$$

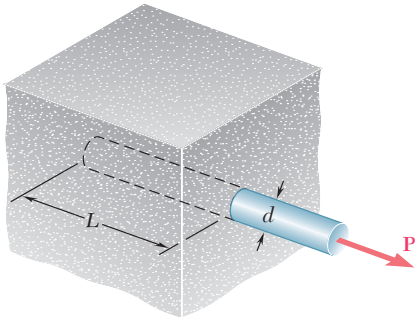
$$F_U = 100 \times 10^3 \text{ N}$$

$$F.S. = \frac{F_U}{F_{BD}} = \frac{100 \times 10^3}{29.014 \times 10^3}$$



$F.S. = 3.45 \blacktriangleleft$

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**PROBLEM 1.68**

A force  $P$  is applied as shown to a steel reinforcing bar that has been embedded in a block of concrete. Determine the smallest length  $L$  for which the full allowable normal stress in the bar can be developed. Express the result in terms of the diameter  $d$  of the bar, the allowable normal stress  $\sigma_{\text{all}}$  in the steel, and the average allowable bond stress  $\tau_{\text{all}}$  between the concrete and the cylindrical surface of the bar. (Neglect the normal stresses between the concrete and the end of the bar.)

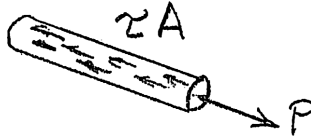
**SOLUTION**

For shear,  $A = \pi dL$   
 $P = \tau_{\text{all}}A = \tau_{\text{all}}\pi dL$

For tension,  $A = \frac{\pi}{4}d^2$   
 $P = \sigma_{\text{all}}A = \sigma_{\text{all}}\left(\frac{\pi}{4}d^2\right)$

Equating,  $\tau_{\text{all}}\pi dL = \sigma_{\text{all}}\frac{\pi}{4}d^2$

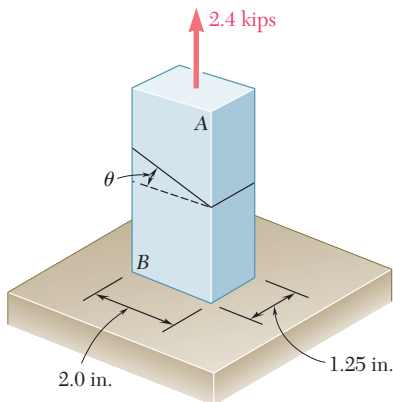
Solving for  $L$ ,



$L_{\text{min}} = \sigma_{\text{all}}d/4\tau_{\text{all}} \blacktriangleleft$

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**PROBLEM 1.69**

The two portions of member  $AB$  are glued together along a plane forming an angle  $\theta$  with the horizontal. Knowing that the ultimate stress for the glued joint is 2.5 ksi in tension and 1.3 ksi in shear, determine (a) the value of  $\theta$  for which the factor of safety of the member is maximum, (b) the corresponding value of the factor of safety. (*Hint:* Equate the expressions obtained for the factors of safety with respect to the normal and shearing stresses.)

**SOLUTION**

$$A_0 = (2.0)(1.25) = 2.50 \text{ in}^2$$

At the optimum angle,  $(F.S.)_\sigma = (F.S.)_\tau$

$$\text{Normal stress: } \sigma = \frac{P}{A_0} \cos^2 \theta \quad \therefore \quad P_{U,\sigma} = \frac{\sigma_U A_0}{\cos^2 \theta}$$

$$(F.S.)_\sigma = \frac{P_{U,\sigma}}{P} = \frac{\sigma_U A_0}{P \cos^2 \theta}$$

$$\text{Shearing stress: } \tau = \frac{P}{A_0} \sin \theta \cos \theta \quad \therefore \quad P_{U,\tau} = \frac{\tau_U A_0}{\sin \theta \cos \theta}$$

$$(F.S.)_\tau = \frac{P_{U,\tau}}{P} = \frac{\tau_U A_0}{P \sin \theta \cos \theta}$$

$$\text{Equating, } \frac{\sigma_U A_0}{P \cos^2 \theta} = \frac{\tau_U A_0}{P \sin \theta \cos \theta}$$

$$\text{Solving, } \frac{\sin \theta}{\cos \theta} = \tan \theta = \frac{\tau_U}{\sigma_U} = \frac{1.3}{2.5} = 0.520$$

$$(a) \quad \theta_{\text{opt}} = 27.5^\circ \quad \blacktriangleleft$$

$$(b) \quad P_U = \frac{\sigma_U A_0}{\cos^2 \theta} = \frac{(2.5)(2.50)}{\cos^2 27.5^\circ} = 7.94 \text{ kips}$$

$$F.S. = \frac{P_U}{P} = \frac{7.94}{2.4}$$

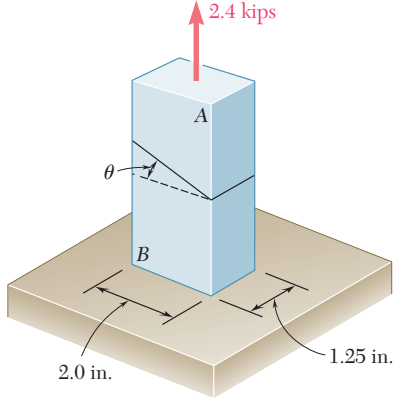
$$F.S. = 3.31 \quad \blacktriangleleft$$

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**PROBLEM 1.70**

The two portions of member  $AB$  are glued together along a plane forming an angle  $\theta$  with the horizontal. Knowing that the ultimate stress for the glued joint is 2.5 ksi in tension and 1.3 ksi in shear, determine the range of values of  $\theta$  for which the factor of safety of the members is at least 3.0.

**SOLUTION**

$$A_0 = (2.0)(1.25) = 2.50 \text{ in.}^2$$

$$P = 2.4 \text{ kips}$$

$$P_U = (F.S.)P = 7.2 \text{ kips}$$

Based on tensile stress,

$$\sigma_U = \frac{P_U}{A_0} \cos^2 \theta$$

$$\cos^2 \theta = \frac{\sigma_U A_0}{P_U} = \frac{(2.5)(2.50)}{7.2} = 0.86806$$

$$\cos \theta = 0.93169 \quad \theta = 21.3^\circ \quad \theta > 21.3^\circ$$

Based on shearing stress,

$$\tau_U = \frac{P_U}{A_0} \sin \theta \cos \theta = \frac{P_U}{2A_0} \sin 2\theta$$

$$\sin 2\theta = \frac{2A_0 \tau_U}{P_U} = \frac{(2)(2.50)(1.3)}{7.2} = 0.90278$$

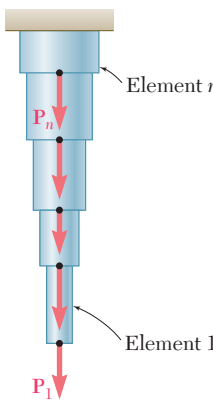
$$2\theta = 64.52^\circ \quad \theta = 32.3^\circ \quad \theta < 32.3^\circ$$

Hence,

$$21.3^\circ < \theta < 32.3^\circ \quad \blacktriangleleft$$

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### PROBLEM 1.C1

A solid steel rod consisting of  $n$  cylindrical elements welded together is subjected to the loading shown. The diameter of element  $i$  is denoted by  $d_i$  and the load applied to its lower end by  $\mathbf{P}_i$  with the magnitude  $P_i$  of this load being assumed positive if  $\mathbf{P}_i$  is directed downward as shown and negative otherwise. (a) Write a computer program that can be used with either SI or U.S. customary units to determine the average stress in each element of the rod. (b) Use this program to solve Problems 1.1 and 1.3.

### SOLUTION

Force in element  $i$ :  
 It is the sum of the forces applied to that element and all lower ones:

$$F_i = \sum_{k=1}^i P_k$$

Average stress in element  $i$ :

$$\text{Area} = A_i = \frac{1}{4} \pi d_i^2$$

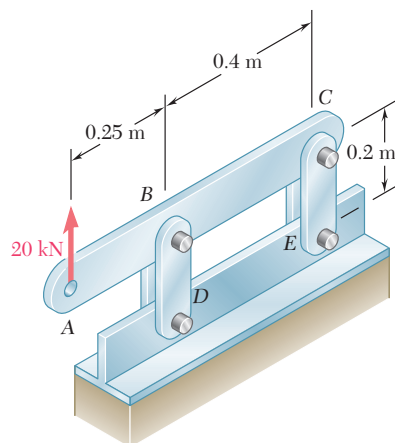
$$\text{Ave. stress} = \frac{F_i}{A_i}$$

Program outputs:

Problem 1.1		Problem 1.3	
Element	Stress (MPa)	Element	Stress (ksi)
1	84.883	1	22.635
2	-96.766	2	17.927

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### PROBLEM 1.C2



A 20-kN load is applied as shown to the horizontal member  $ABC$ . Member  $ABC$  has a  $10 \times 50$ -mm uniform rectangular cross section and is supported by four vertical links, each of  $8 \times 36$ -mm uniform rectangular cross section. Each of the four pins at  $A$ ,  $B$ ,  $C$ , and  $D$  has the same diameter  $d$  and is in double shear. (a) Write a computer program to calculate for values of  $d$  from 10 to 30 mm, using 1-mm increments, (i) the maximum value of the average normal stress in the links connecting pins  $B$  and  $D$ , (ii) the average normal stress in the links connecting pins  $C$  and  $E$ , (iii) the average shearing stress in pin  $B$ , (iv) the average shearing stress in pin  $C$ , (v) the average bearing stress at  $B$  in member  $ABC$ , and (vi) the average bearing stress at  $C$  in member  $ABC$ . (b) Check your program by comparing the values obtained for  $d = 16$  mm with the answers given for Probs. 1.7 and 1.27. (c) Use this program to find the permissible values of the diameter  $d$  of the pins, knowing that the allowable values of the normal, shearing, and bearing stresses for the steel used are, respectively, 150 MPa, 90 MPa, and 230 MPa. (d) Solve Part c, assuming that the thickness of member  $ABC$  has been reduced from 10 to 8 mm.

### SOLUTION

#### Forces in links.

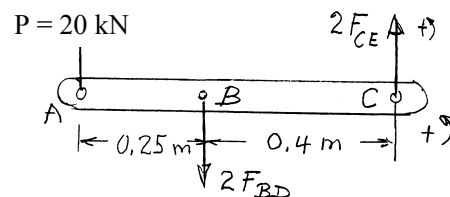
*F.B.* diagram of  $ABC$ :

$$+\circlearrowleft \sum M_C = 0: 2F_{BD}(BC) - P(AC) = 0$$

$$F_{BD} = P(AC)/2(BC) \quad (\text{tension})$$

$$+\circlearrowleft \sum M_B = 0: 2F_{CE}(BC) - P(AB) = 0$$

$$F_{CE} = P(AB)/2(BC) \quad (\text{comp.})$$



(i) Link  $BD$ .

Thickness =  $t_L$

$$A_{BD} = t_L(w_L - d)$$

$$\sigma_{BD} = +F_{BD}/A_{BD}$$

(iii) Pin  $B$ .

$$\tau_B = F_{BD}/(\pi d^2/4)$$

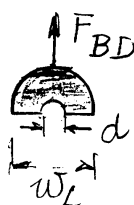
(v) Bearing stress at  $B$ .

Thickness of member  $AC = t_{AC}$

$$\text{Sig Bear } B = F_{BD}/(dt_{AC})$$

(vi) Bearing stress at  $C$ .

$$\text{Sig Bear } C = F_{CE}/(dt_{AC})$$



(ii) Link  $CE$ .

Thickness =  $t_L$

$$A_{CE} = t_L w_L$$

$$\sigma_{CE} = -F_{CE}/A_{CE}$$

(iv) Pin  $C$ .

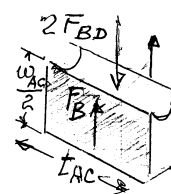
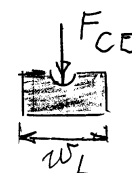
$$\tau_C = F_{CE}/(\pi d^2/4)$$

Shearing stress in  $ABC$  under Pin  $B$ .

$$F_B = \tau_{AC} t_{AC} (w_{AC}/2)$$

$$\sum F_y = 0: 2F_B = 2F_{BD}$$

$$\tau_{AC} = \frac{2F_{BD}}{\tau_{AC} w_{AC}}$$



**PROBLEM 1.C2 (Continued)**

**Program Outputs**

Input data for Parts (a), (b), (c):

$$P = 20 \text{ kN}, \quad AB = 0.25 \text{ m}, \quad BC = 0.40 \text{ m}, \quad AC = 0.65 \text{ m},$$

$$TL = 8 \text{ mm}, \quad WL = 36 \text{ mm}, \quad TAC = 10 \text{ mm}, \quad WAC = 50 \text{ mm}$$

d	Sigma BD	Sigma CE	Tau B	Tau C	SigBear B	SigBear C
10.00	78.13	-21.70	<del>206.90</del>	79.58	<del>325.00</del>	125.00
11.00	81.25	-21.70	<del>170.99</del>	65.77	<del>295.45</del>	113.64
12.00	84.64	-21.70	<del>143.68</del>	55.26	<del>270.83</del>	104.17
13.00	88.32	-21.70	<del>122.43</del>	47.09	<del>250.00</del>	96.15
14.00	92.33	-21.70	<del>105.56</del>	40.60	<del>232.14</del>	89.29
15.00	96.73	-21.70	<del>91.96</del>	35.37	216.67	83.33
16.00	101.56	-21.70	80.82	31.08	203.12	78.13 ← (b)
17.00	106.91	-21.70	71.59	27.54	191.18	73.53
18.00	112.85	-21.70	63.86	24.56	180.56	69.44
19.00	119.49	-21.70	57.31	22.04	171.05	65.79
20.00	126.95	-21.70	51.73	19.89	162.50	62.50
21.00	135.42	-21.70	46.92	18.04	154.76	59.52
22.00	145.09	-21.70	42.75	16.44	147.73	56.82
23.00	<del>156.25</del>	-21.70	39.11	15.04	141.30	54.35
24.00	<del>169.27</del>	-21.70	35.92	13.82	135.42	52.08
25.00	<del>184.66</del>	-21.70	33.10	12.73	130.00	50.00
26.00	<del>203.13</del>	-21.70	30.61	11.77	125.00	48.08
27.00	<del>225.69</del>	-21.70	28.38	10.92	120.37	46.30
28.00	<del>253.91</del>	-21.70	26.39	10.15	116.07	44.64
29.00	<del>290.18</del>	-21.70	24.60	9.46	112.07	43.10
30.00	<del>338.54</del>	-21.70	22.99	8.84	108.33	41.67

(c) Answer:  $16 \text{ mm} \leq d \leq 22 \text{ mm}$  ◀ (c)

Check: For  $d = 22 \text{ mm}$ ,  $\text{Tau } AC = 65 \text{ MPa} < 90 \text{ MPa}$  O.K.



**PROBLEM 1.C2 (Continued)**

Input data for Part (d):  $P = 20$  kN,

$$AB = 0.25 \text{ m}, \quad BC = 0.40 \text{ m},$$

$$AC = 0.65 \text{ m}, \quad TL = 8 \text{ mm}, \quad WL = 36 \text{ mm},$$

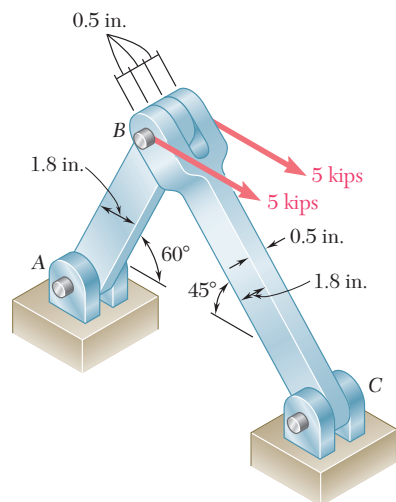
$$TAC = 8 \text{ mm}, \quad WAC = 50 \text{ mm}$$

d	Sigma BD	Sigma CE	Tau B	Tau C	SigBear B	SigBear C
10.00	78.13	-21.70	206.90	79.58	406.25	156.25
11.00	81.25	-21.70	170.99	65.77	369.32	142.05
12.00	84.64	-21.70	143.68	55.26	338.54	130.21
13.00	88.32	-21.70	122.43	47.09	312.50	120.19
14.00	92.33	-21.70	105.56	40.60	290.18	111.61
15.00	96.73	-21.70	91.96	35.37	270.83	104.17
16.00	101.56	-21.70	80.82	31.08	253.91	97.66
17.00	106.91	-21.70	71.59	27.54	238.97	91.91
18.00	112.85	-21.70	63.86	24.56	225.69	86.81
19.00	119.49	-21.70	57.31	22.04	213.82	82.24
20.00	126.95	-21.70	51.73	19.89	203.12	78.13
21.00	135.42	-21.70	46.92	18.04	193.45	74.40
22.00	145.09	-21.70	42.75	16.44	184.66	71.02
23.00	156.25	-21.70	39.11	15.04	176.63	67.93
24.00	169.27	-21.70	35.92	13.82	169.27	65.10
25.00	184.66	-21.70	33.10	12.73	162.50	62.50
26.00	203.13	-21.70	30.61	11.77	156.25	60.10
27.00	225.69	-21.70	28.38	10.92	150.46	57.87
28.00	253.91	-21.70	26.39	10.15	145.09	55.80
29.00	290.18	-21.70	24.60	9.46	140.09	53.88
30.00	338.54	-21.70	22.99	8.84	135.42	52.08

(d) Answer:  $18 \text{ mm} \leq d \leq 22 \text{ mm}$  ◀ (d)

Check: For  $d = 22$  mm,  $\text{Tau } AC = 81.25 \text{ MPa} < 90 \text{ MPa}$  O.K.

### PROBLEM 1.C3



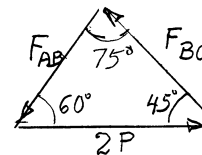
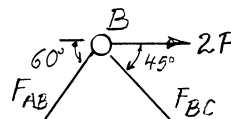
Two horizontal 5-kip forces are applied to Pin  $B$  of the assembly shown. Each of the three pins at  $A$ ,  $B$ , and  $C$  has the same diameter  $d$  and is double shear. (a) Write a computer program to calculate for values of  $d$  from 0.50 to 1.50 in., using 0.05-in. increments, (i) the maximum value of the average normal stress in member  $AB$ , (ii) the average normal stress in member  $BC$ , (iii) the average shearing stress in pin  $A$ , (iv) the average shearing stress in pin  $C$ , (v) the average bearing stress at  $A$  in member  $AB$ , (vi) the average bearing stress at  $C$  in member  $BC$ , and (vii) the average bearing stress at  $B$  in member  $BC$ . (b) Check your program by comparing the values obtained for  $d = 0.8$  in. with the answers given for Problems 1.60 and 1.61. (c) Use this program to find the permissible values of the diameter  $d$  of the pins, knowing that the allowable values of the normal, shearing, and bearing stresses for the steel used are, respectively, 22 ksi, 13 ksi, and 36 ksi. (d) Solve Part c, assuming that a new design is being investigated in which the thickness and width of the two members are changed, respectively, from 0.5 to 0.3 in. and from 1.8 to 2.4 in.

### SOLUTION

Forces in members  $AB$  and  $BC$ .

Free body: Pin  $B$ .

From force triangle:



$$\frac{F_{AB}}{\sin 45^\circ} = \frac{F_{BC}}{\sin 60^\circ} = \frac{2P}{\sin 75^\circ}$$

$$F_{AB} = 2P(\sin 45^\circ / \sin 75^\circ)$$

$$F_{BC} = 2P(\sin 60^\circ / \sin 75^\circ)$$

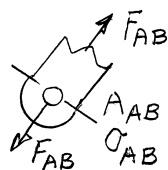
(i) Max. ave. stress in  $AB$ .

Width =  $w$

Thickness =  $t$

$$A_{AB} = (w - d)t$$

$$\sigma_{AB} = F_{AB} / A_{AB}$$



(iii) Pin  $A$ .

$$\tau_A = (F_{AB}/2) / (\pi d^2/4)$$

(v) Bearing stress at  $A$ .

$$\text{Sig Bear } A = F_{AB}/dt$$

(vii) Bearing stress at  $B$  in member  $BC$ .

$$\text{Sig Bear } B = F_{BC}/2dt$$

(ii) Ave. stress in  $BC$ .

$$A_{BC} = wt$$

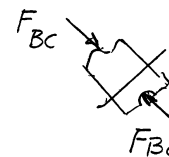
$$\sigma_{BC} = F_{BC} / A_{BC}$$

(iv) Pin  $C$ .

$$\tau_C = (F_{BC}/2) / (\pi d^2/4)$$

(vi) Bearing stress at  $C$ .

$$\text{Sig Bear } C = F_{BC}/dt$$



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**PROBLEM 1.C3 (Continued)**

**Program Outputs**

Input data for Parts (a), (b), (c):

$$P = 5 \text{ kips}, \quad w = 1.8 \text{ in.}, \quad t = 0.5 \text{ in.}$$

D in.	SIGAB ksi	SIGBC ksi	TAUA ksi	TAUC ksi	SIGBRGA ksi	SIGBRGC ksi	SIGBRGB ksi
0.500	11.262	-9.962	<del>18.642</del>	<del>22.831</del>	29.282	35.863	17.932
0.550	11.713	-9.962	<del>15.408</del>	<del>18.869</del>	26.620	32.603	16.301
0.600	12.201	-9.962	12.945	<del>15.855</del>	24.402	29.886	14.943
0.650	12.731	-9.962	11.030	<del>12.510</del>	22.525	27.587	13.793
0.700	13.310	-9.962	9.511	<del>11.649</del>	20.916	25.616	12.808
0.750	13.944	-9.962	8.285	10.147	19.521	23.909	11.954
0.800	14.641	-9.962	7.282	8.918	18.301	22.414	11.207
0.850	15.412	-9.962	6.450	7.900	17.225	21.096	10.548
0.900	16.268	-9.962	5.754	7.047	16.268	19.924	9.962
0.950	17.225	-9.962	5.164	6.324	15.412	18.875	9.438
1.000	18.301	-9.962	4.660	5.708	14.641	17.932	8.966
1.050	19.521	-9.962	4.227	5.177	13.944	17.078	8.539
1.100	20.916	-9.962	3.852	4.717	13.310	16.301	8.151
1.150	<del>22.525</del>	-9.962	3.524	4.316	12.731	15.593	7.796
1.200	<del>24.402</del>	-9.962	3.236	3.964	12.201	14.943	7.471
1.250	<del>26.620</del>	-9.962	2.983	3.653	11.713	14.345	7.173
1.300	<del>29.282</del>	-9.962	2.758	3.377	11.262	13.793	6.897
1.350	<del>32.536</del>	-9.962	2.557	3.132	10.845	13.283	6.641
1.400	<del>36.603</del>	-9.962	2.378	2.912	10.458	12.808	6.404
1.450	<del>41.831</del>	-9.962	2.217	2.715	10.097	12.367	6.183
1.500	<del>48.803</del>	-9.962	2.071	2.537	9.761	11.954	5.977

← (b)

(c) Answer:  $0.70 \text{ in.} \leq d \leq 1.10 \text{ in.}$  ◀ (c)

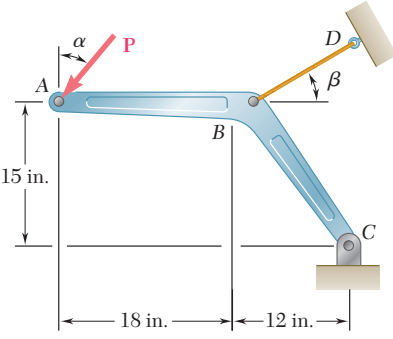
**PROBLEM 1.C3 (Continued)**

Input data for Part (d),

$$P = 5 \text{ kips}, \quad w = 2.4 \text{ in.}, \quad t = 0.3 \text{ in.}$$

D in.	SIGAB ksi	SIGBC ksi	TAUA ksi	TAUC ksi	SIGBRGA ksi	SIGBRGC ksi	SIGBRGB ksi
0.500	12.843	-12.452	<del>18.642</del>	<del>22.831</del>	<del>46.803</del>	<del>59.772</del>	29.886
0.550	13.190	-12.452	<del>15.406</del>	<del>18.869</del>	<del>44.367</del>	<del>54.338</del>	27.169
0.600	13.556	-12.452	<del>12.945</del>	<del>15.855</del>	<del>40.689</del>	<del>49.810</del>	24.905
0.650	13.944	-12.452	11.030	<del>13.510</del>	<del>37.541</del>	<del>45.978</del>	22.989
0.700	14.354	-12.452	9.511	11.649	34.860	<del>42.694</del>	21.347
0.750	14.789	-12.452	8.285	10.147	32.536	<del>39.848</del>	19.924
0.800	15.251	-12.452	7.282	8.918	30.502	<del>37.357</del>	18.679
0.850	15.743	-12.452	6.450	7.900	28.708	35.160	17.580
0.900	16.268	-12.452	5.754	7.047	27.113	33.206	16.603
0.950	16.829	-12.452	5.164	6.324	25.686	31.459	15.729
1.000	17.430	-12.452	4.660	5.708	24.402	29.886	14.943
1.050	18.075	-12.452	4.227	5.177	23.240	28.463	14.231
1.100	18.771	-12.452	3.852	4.717	22.183	27.169	13.584
1.150	19.521	-12.452	3.524	4.316	21.219	25.988	12.994
1.200	20.335	-12.452	3.236	3.964	20.335	24.905	12.452
1.250	21.219	-12.452	2.983	3.653	19.521	23.909	11.954
1.300	<del>22.183</del>	-12.452	2.758	3.377	18.771	22.989	11.495
1.350	<del>23.240</del>	-12.452	2.557	3.132	18.075	22.138	11.069
1.400	<del>24.402</del>	-12.452	2.378	2.912	17.430	21.347	10.674
1.450	<del>25.686</del>	-12.452	2.217	2.715	16.829	20.611	10.305
1.500	<del>27.113</del>	-12.452	2.071	2.537	16.268	19.924	9.962

(d) Answer:  $0.85 \text{ in.} \leq d \leq 1.25 \text{ in.}$  ◀ (d)



### PROBLEM 1.C4

A 4-kip force  $P$  forming an angle  $\alpha$  with the vertical is applied as shown to member  $ABC$ , which is supported by a pin and bracket at  $C$  and by a cable  $BD$  forming an angle  $\beta$  with the horizontal. (a) Knowing that the ultimate load of the cable is 25 kips, write a computer program to construct a table of the values of the factor of safety of the cable for values of  $\alpha$  and  $\beta$  from 0 to  $45^\circ$ , using increments in  $\alpha$  and  $\beta$  corresponding to 0.1 increments in  $\tan \alpha$  and  $\tan \beta$ . (b) Check that for any given value of  $\alpha$ , the maximum value of the factor of safety is obtained for  $\beta = 38.66^\circ$  and explain why. (c) Determine the smallest possible value of the factor of safety for  $\beta = 38.66^\circ$ , as well as the corresponding value of  $\alpha$ , and explain the result obtained.

### SOLUTION

(a) Draw *F.B.* diagram of *ABC*:

$$+\circlearrowleft \Sigma M_C = 0: (P \sin \alpha)(15 \text{ in.}) + (P \cos \alpha)(30 \text{ in.}) - (F \cos \beta)(15 \text{ in.}) - (F \sin \beta)(12 \text{ in.}) = 0$$

$$F = P \frac{15 \sin \alpha + 30 \cos \alpha}{15 \cos \beta + 12 \sin \beta}$$

$$F.S. = F_{ult}/F$$

Output for  $P = 4$  kips and  $F_{ult} = 20$  kips:

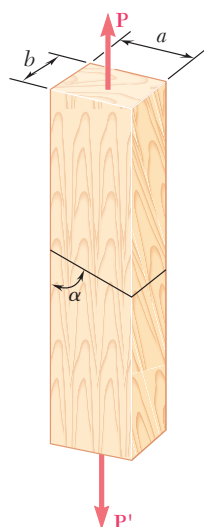
		VALUES OF FS										
		BETA										
ALPHA		0	5.71	11.31	16.70	21.80	26.56	30.96	34.99	38.66	41.99	45.00
0.000	3.125	3.358	3.555	3.712	3.830	3.913	3.966	3.994	4.002	3.995	3.977	
5.711	2.991	3.214	3.402	3.552	3.666	3.745	3.796	3.823	3.830	3.824	3.807	
11.310	2.897	3.113	3.295	3.441	3.551	3.628	3.677	3.703	3.710	3.704	3.687	
16.699	2.837	3.049	3.227	3.370	3.477	3.553	3.600	3.626	3.633	3.627	3.611	
21.801	2.805	3.014	3.190	3.331	3.438	3.512	3.560	3.585	3.592	3.586	3.570	
26.565	2.795	3.004	3.179	3.320	3.426	3.500	3.547	3.572	3.579	3.573	3.558	
30.964	2.803	3.013	3.189	3.330	3.436	3.510	3.558	3.583	3.590	3.584	3.568	
34.992	2.826	3.036	3.214	3.356	3.463	3.538	3.586	3.611	3.619	3.612	3.596	
38.660	2.859	3.072	3.252	3.395	3.503	3.579	3.628	3.653	3.661	3.655	3.638	
41.987	2.899	3.116	3.298	3.444	3.554	3.631	3.680	3.706	3.713	3.707	3.690	
45.000	2.946	3.166	3.351	3.499	3.611	3.689	3.739	3.765	3.773	3.767	3.750	

↑(b)

(b) When  $\beta = 38.66^\circ$ ,  $\tan \beta = 0.8$  and cable  $BD$  is perpendicular to the lever arm  $BC$ .

(c)  $F.S. = 3.579$  for  $\alpha = 26.6^\circ$ ;  $P$  is perpendicular to the lever arm  $AC$ .

*Note:* The value  $F.S. = 3.579$  is the smallest of the values of  $F.S.$  corresponding to  $\beta = 38.66^\circ$  and the largest of those corresponding to  $\alpha = 26.6^\circ$ . The point  $\alpha = 26.6^\circ$ ,  $\beta = 38.66^\circ$  is a "saddle point," or "minimax" of the function  $F.S.(\alpha, \beta)$ .



### PROBLEM 1.C5

A load  $P$  is supported as shown by two wooden members of uniform rectangular cross section that are joined by a simple glued scarf splice. (a) Denoting by  $\sigma_U$  and  $\tau_U$ , respectively, the ultimate strength of the joint in tension and in shear, write a computer program which, for given values of  $a$ ,  $b$ ,  $P$ ,  $\sigma_U$  and  $\tau_U$ , expressed in either SI or U.S. customary units, and for values of  $\alpha$  from  $5^\circ$  to  $85^\circ$  at  $5^\circ$  intervals, can be used to calculate (i) the normal stress in the joint, (ii) the shearing stress in the joint, (iii) the factor of safety relative to failure in tension, (iv) the factor of safety relative to failure in shear, and (v) the overall factor of safety for the glued joint. (b) Apply this program, using the dimensions and loading of the members of Probs. 1.29 and 1.31, knowing that  $\sigma_U = 150$  psi and  $\tau_U = 214$  psi for the glue used in Prob. 1.29, and that  $\sigma_U = 1.26$  MPa and  $\tau_U = 1.50$  MPa for the glue used in Prob. 1.31. (c) Verify in each of these two cases that the shearing stress is maximum for  $\alpha = 45^\circ$ .

### SOLUTION

(i) and (ii) Draw the *F.B.* diagram of lower member:

$$\begin{aligned} \downarrow \sum F_x = 0: \quad -V + P \cos \alpha = 0 & \quad V = P \cos \alpha \\ + \uparrow \sum F_y = 0: \quad F - P \sin \alpha = 0 & \quad F = P \sin \alpha \end{aligned}$$

Area =  $ab/\sin \alpha$

Normal stress: 
$$\sigma = \frac{F}{\text{Area}} = (P/ab) \sin^2 \alpha$$

Shearing stress: 
$$\tau = \frac{V}{\text{Area}} = (P/ab) \sin \alpha \cos \alpha$$

(iii) *F.S.* for tension (normal stresses):

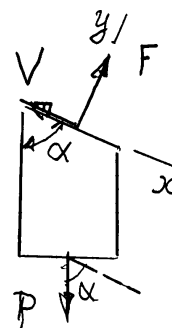
$$FSN = \sigma_U / \sigma$$

(iv) *F.S.* for shear:

$$FSS = \tau_U / \tau$$

(v) Overall *F.S.*:

$$F.S. = \text{The smaller of } FSN \text{ and } FSS.$$



**PROBLEM 1.C5 (Continued)****Program Outputs****Problem 1.29**

$$a = 150 \text{ mm}$$

$$b = 75 \text{ mm}$$

$$P = 11 \text{ kN}$$

$$\sigma_U = 1.26 \text{ MPa}$$

$$\tau_U = 1.50 \text{ MPa}$$

ALPHA	SIG (MPa)	TAU (MPa)	FSN	FSS	FS
5	0.007	0.085	169.644	17.669	17.669
10	0.029	0.167	42.736	8.971	8.971
15	0.065	0.244	19.237	6.136	6.136
20	0.114	0.314	11.016	4.773	4.773
25	0.175	0.375	7.215	4.005	4.005
30	0.244	0.423	5.155	3.543	3.543
35	0.322	0.459	3.917	3.265	3.265
40	0.404	0.481	3.119	3.116	3.116
45	0.489	0.489	2.577	3.068	2.577
50	0.574	0.481	2.196	3.116	2.196
55	0.656	0.459	1.920	3.265	1.920
60	0.733	0.423	1.718	3.543	1.718
65	0.803	0.375	1.569	4.005	1.569
70	0.863	0.314	1.459	4.773	1.459
75	0.912	0.244	1.381	6.136	1.381
80	0.948	0.167	1.329	8.971	1.329
85	0.970	0.085	1.298	17.669	1.298

◀ (b), (c)

Full file at <https://TestbankDirect.eu/>**PROBLEM 1.C5 (Continued)**Problem 1.31

$$a = 5 \text{ in.}$$

$$b = 3 \text{ in.}$$

$$P = 1400 \text{ lb}$$

$$\sigma_U = 150 \text{ psi}$$

$$\tau_U = 214 \text{ psi}$$

ALPHA	SIG (psi)	TAU (psi)	FSN	FSS	FS	
5	0.709	8.104	211.574	26.408	26.408	
10	2.814	15.961	53.298	13.408	13.408	
15	6.252	23.333	23.992	9.171	9.171	
20	10.918	29.997	13.739	7.134	7.134	
25	16.670	35.749	8.998	5.986	5.986	
30	23.333	40.415	6.429	5.295	5.295	
35	30.706	43.852	4.885	4.880	4.880	
40	38.563	45.958	3.890	4.656	3.890	
45	46.667	46.667	3.214	4.586	3.214	◀ (c)
50	54.770	45.958	2.739	4.656	2.739	
55	62.628	43.852	2.395	4.880	2.395	
60	70.000	40.415	2.143	5.295	2.143	◀ (b)
65	76.663	35.749	1.957	5.986	1.957	
70	82.415	29.997	1.820	7.134	1.820	
75	87.081	23.333	1.723	9.171	1.723	
80	90.519	15.961	1.657	13.408	1.657	
85	92.624	8.104	1.619	26.408	1.619	

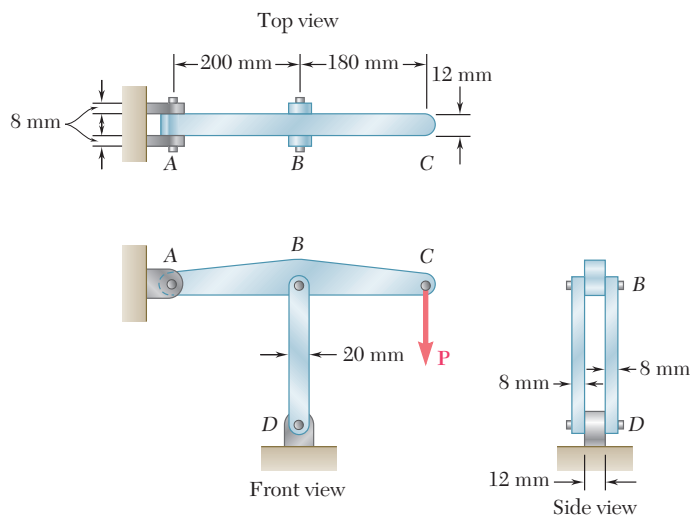
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**PROBLEM 1.C6**



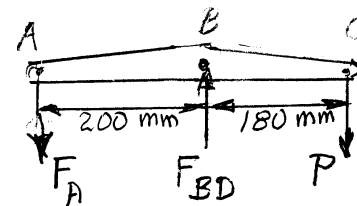
Member  $ABC$  is supported by a pin and bracket at  $A$  and by two links, which are pin-connected to the member at  $B$  and to a fixed support at  $D$ . (a) Write a computer program to calculate the allowable load  $P_{all}$  for any given values of (i) the diameter  $d_1$  of the pin at  $A$ , (ii) the common diameter  $d_2$  of the pins at  $B$  and  $D$ , (iii) the ultimate normal stress  $\sigma_U$  in each of the two links, (iv) the ultimate shearing stress  $\tau_U$  in each of the three pins, and (v) the desired overall factor of safety  $F.S.$  (b) Your program should also indicate which of the following three stresses is critical: the normal stress in the links, the shearing stress in the pin at  $A$ , or the shearing stress in the pins at  $B$  and  $D$ . (c) Check your program by using the data of Probs. 1.55 and 1.56, respectively, and comparing the answers obtained for  $P_{all}$  with those given in the text. (d) Use your program to determine the allowable load  $P_{all}$ , as well as which of the stresses is critical, when  $d_1 = d_2 = 15$  mm,  $\sigma_U = 110$  MPa for aluminum links,  $\tau_U = 100$  MPa for steel pins, and  $F.S. = 3.2$ .

**SOLUTION**

(a) F.B. diagram of ABC:

$$\Sigma M_A = 0: P = \frac{200}{380} F_{BD}$$

$$\Sigma M_B = 0: P = \frac{200}{180} F_A$$



(i) For given  $d_1$  of Pin A:  $F_A = 2(\tau_U/F.S.)(\pi d_1^2/4), P_1 = \frac{200}{180} F_A$

(ii) For given  $d_2$  of Pins B and D:  $F_{BD} = 2(\tau_U/F.S.)(\pi d_2^2/4), P_2 = \frac{200}{380} F_{BD}$

(iii) For ultimate stress in links BD:  $F_{BD} = 2(\sigma_U/F.S.)(0.02)(0.008), P_3 = \frac{200}{380} F_{BD}$

(iv) For ultimate shearing stress in pins:  $P_4$  is the smaller of  $P_1$  and  $P_2$ .

(v) For desired overall F.S.:  $P_5$  is the smaller of  $P_3$  and  $P_4$ .

If  $P_3 < P_4$ , stress is critical in links.

If  $P_4 < P_3$  and  $P_1 < P_2$ , stress is critical in Pin A.

If  $P_4 < P_3$  and  $P_2 < P_1$ , stress is critical in Pins B and D.

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Full file at <https://TestbankDirect.eu/>**PROBLEM 1.C6 (Continued)****Program Outputs**

(b) Problem 1.55. Data:  $d_1 = 8 \text{ mm}$ ,  $d_2 = 12 \text{ mm}$ ,  $\sigma_U = 250 \text{ MPa}$ ,  $\tau_U = 100 \text{ MPa}$ ,  $F.S. = 3.0$

$P_{\text{all}} = 3.72 \text{ kN}$ . Stress in Pin  $A$  is critical. ◀

(c) Problem 1.56. Data:  $d_1 = 10 \text{ mm}$ ,  $d_2 = 12 \text{ mm}$ ,  $\sigma_U = 250 \text{ MPa}$ ,  $\tau_U = 100 \text{ MPa}$ ,  $F.S. = 3.0$

$P_{\text{all}} = 3.97 \text{ kN}$ . Stress in Pins  $B$  and  $D$  is critical. ◀

(d) Data:  $d_1 = d_2 = 15 \text{ mm}$ ,  $\sigma_U = 110 \text{ MPa}$ ,  $\tau_U = 100 \text{ MPa}$ ,  $F.S. = 3.2$

$P_{\text{all}} = 5.79 \text{ kN}$ . Stress in links is critical. ◀

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