

Q1 (8 points). For the system of figure (1), determine the values of K , and a such as the overall system has a damping of 0.7 and undamped natural frequency of 4 rad/sec.

$\omega_n = 4$

0.732

0.175, 16

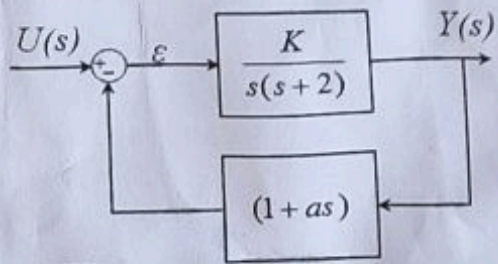


Figure (1)

Q2 (12 points). For the system of figure (2-a) the forcing function F is a step input of 2 Newton. Knowing that the transfer function of the system is $\frac{X(s)}{F(s)} = \frac{1}{ms^2 + bs + k}$ where m is the mass of the body, k is the spring constant and b is the friction coefficient. If the response of the system was the function of the figure (2-b) find m , b and k .

20. ω_n
 5.70
 $k = 50$

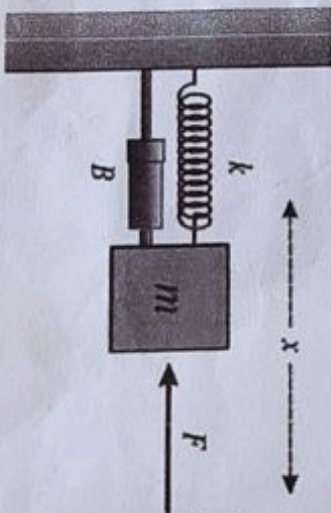


Figure (2-a)

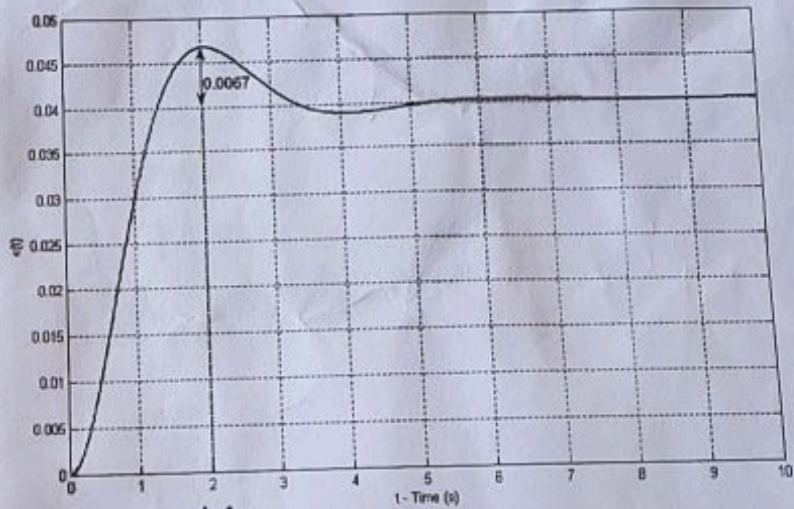


Figure (2-b)

Q3 (8 points). Find the overall transfer function for the system given in Figure (3)

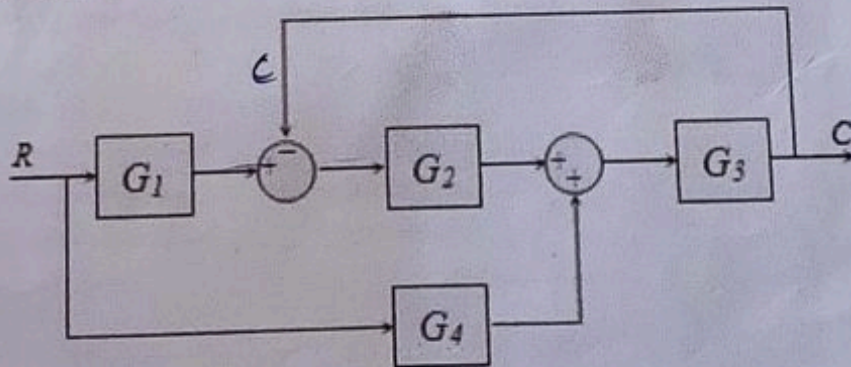


Figure (3)

Q4 (4 points). For a second order system described by the transfer function $G(s) = \frac{2}{(s^2 + 3s + 12)}$,

determine the rise time and the peak time and the maximum overshoot for the system's response to a unit step input.

fr 0.646 $t_p = 1.006$ $\sigma = 0.22$

Q5 (12 points). Consider the cascaded liquid storage tanks shown in figure (5). The differential equation describing the behaviour of the first tank is given as $h_1'(t) = 8(F_{in}(t) - F_{12}(t))$ and the differential equation describing the behaviour of second tank is given as $h_2'(t) = 10(F_{12}(t) - F_{out}(t))$. The first tank output flow rate is given as $F_{12}(t) = 0.0625 h_1(t)$ and the second tank output flow rate is given as $F_{out}(t) = 0.05 h_2(t)$. Assuming that the two tanks were empty at initial time, find the following:

- The transfer function that relates h_1 to F_{in} .
- The transfer function that relates h_2 to F_{12} .
- The transfer function that relates h_2 to F_{in} .
- Find $h_2(t)$, if $F_{in}(t)$ is a unit step signal.
- The time constant of the first tank, and the time constant of the dynamic between $h_2(t)$ and $F_{in}(t)$.

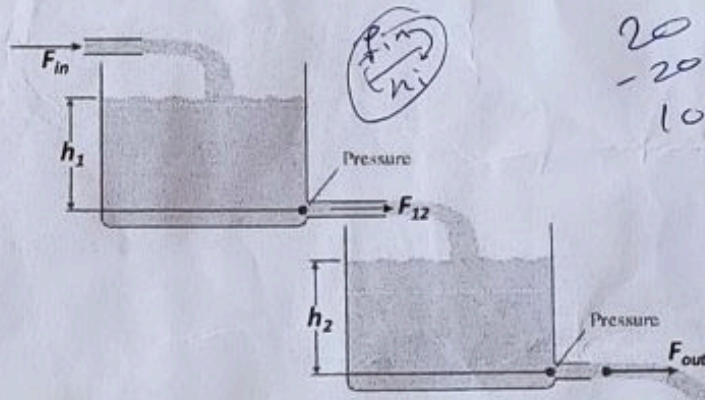


Figure (5)

Q6 (6 points). Consider the system described by the block diagram of the figure (2) with $G(s) = \frac{9}{s^2 + 3s + 8}$, and $H(s) = \frac{1}{9}$.

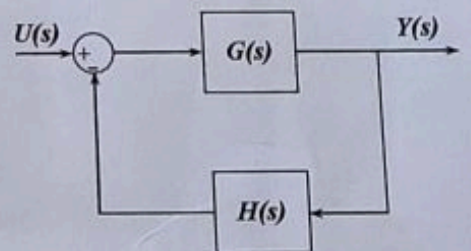


Figure (2)

- Find the overall transfer function of this system.
- If the input function is a unit step function find:
 - the rise time of the output signal *0.806*
 - the peak time of the output signal *1.127*
 - the maximum overshoot of the output signal *0.163*
 - the setting time for an allowable tolerance of 5% *2*

1/4 = 0.25