

Q1 (8 points). For the system of figure (1), determine the values of  $K$ , and  $a$  such as the overall system has a damping of 0.7 and undamped natural frequency of 4 rad/sec.

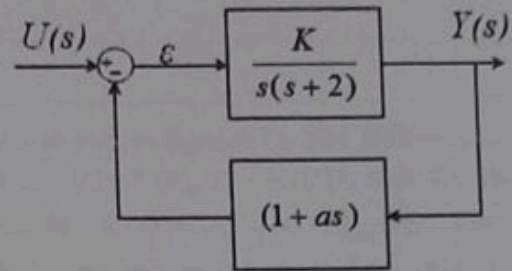


Figure (1)

Q2 (12 points). For the system of figure (2-a) the forcing function  $F$  is a step input of 2 Newton. Knowing that the transfer function of the system is  $\frac{X(s)}{F(s)} = \frac{1}{ms^2 + bs + k}$  where  $m$  is the mass of the body,  $k$  is the spring constant and  $b$  is the friction coefficient. If the response of the system was the function of the figure (2-b) find  $m$ ,  $b$  and  $k$ .

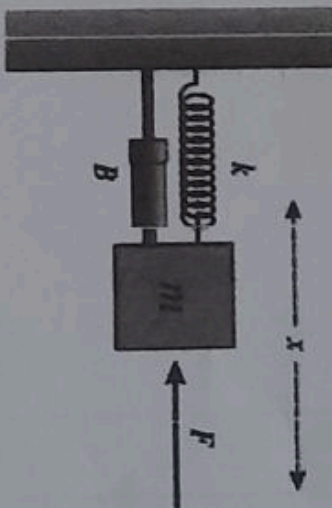


Figure (2-a)

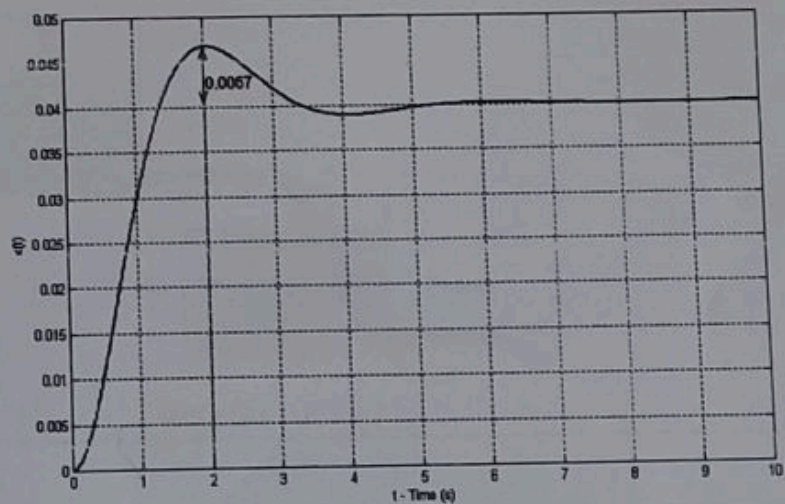


Figure (2-b)

Q3 (8 points). Find the overall transfer function for the system given in Figure (3)

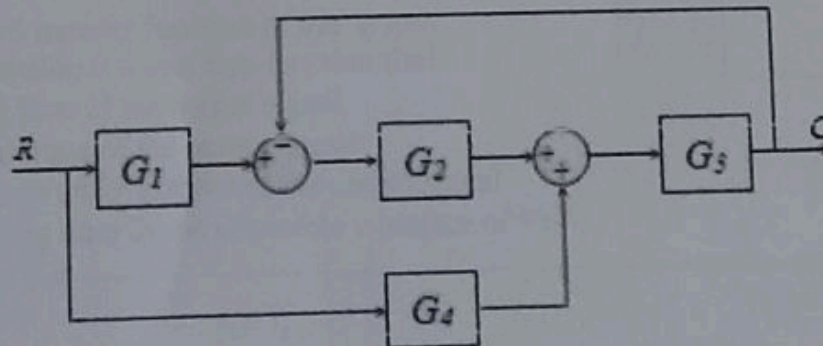


Figure (3)

**Q4 (4 points).** For a second order system described by the transfer function  $G(s) = \frac{2}{(s^2 + 3s + 12)}$ , determine the rise time and the peak time and the maximum overshoot for the system's response to a unit step input.

**Q5 (12 points).** Consider the cascaded liquid storage tanks shown in figure (5). The differential equation describing the behaviour of the first tank is given as  $h_1'(t) = 8(F_{in}(t) - F_{12}(t))$  and the differential equation describing the behaviour of second tank is given as  $h_2'(t) = 10(F_{12}(t) - F_{out}(t))$ . The first tank output flow rate is given as  $F_{12}(t) = 0.0625 h_1(t)$  and the second tank output flow rate is given as  $F_{out}(t) = 0.05 h_2(t)$ . Assuming that the two tanks were empty at initial time, find the following:

- The transfer function that relates  $h_1$  to  $F_{in}$ .
- The transfer function that relates  $h_2$  to  $F_{12}$ .
- The transfer function that relates  $h_2$  to  $F_{in}$ .
- Find  $h_2(t)$ , if  $F_{in}(t)$  is a unit step signal.
- The time constant of the first tank, and the time constant of the dynamic between  $h_2(t)$  and  $F_{in}(t)$ .

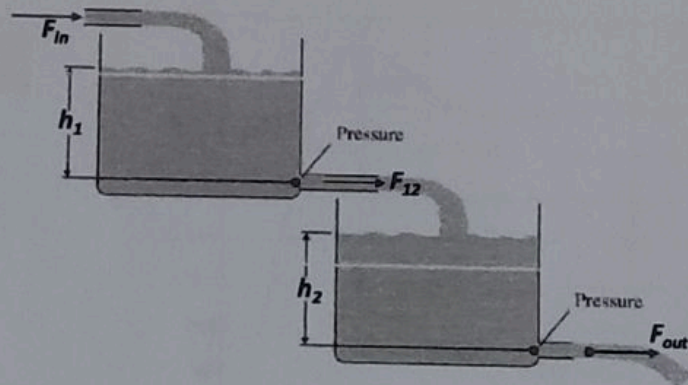


Figure (5)

**Q6 (6 points).** Consider the system described by the block diagram of the figure (2) with  $G(s) = \frac{9}{s^2 + 3s + 8}$ , and  $H(s) = \frac{1}{9}$ .

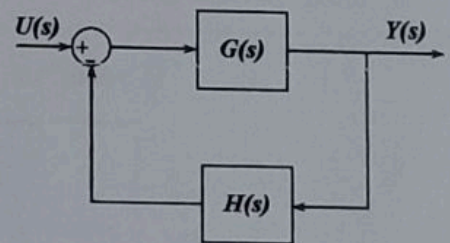


Figure (2)

- Find the overall transfer function of this system.
- If the input function is a unit step function find:
  - the rise time of the output signal
  - the peak time of the output signal
  - the maximum overshoot of the output signal
  - the setting time for an allowable tolerance of 5%